#### Steve Brown, Economist

B. A. in History, University of Colorado

Ph.D. and M.A. in International Relations with a specialty in International Economics. University of Denver

M.S. in Regulatory Economics, University of Wyoming

Twenty-five years of experience with the Public Utility industry:

1979 - 1982	Tri-State Generation and Transmission Association - Power Requirements Supervisor & Rate Specialist
1982 - 1984	Arizona Electric Cooperative - Rate Analyst
1984 - 1986	Houston Lighting & Power - Supervisor of Rate Design
1986 - 1995	Iowa Utilities Board - Chief of the Bureau of Energy Efficiency- Auditing, Research & Utilities Specialist
1995 - Present	Office of the Attorney General for the State of Tennessee - Consumer Advocate and Protection Division - Economist

Oral and written testimony in numerous rate proceedings before the TPSC and the Tennessee Regulatory Authority. Including the following dockets and/or companies

### **Dockets**

TRA # 04-00034 Petition of Chattanooga Gas to Adjust Rates

Testimony Address: <a href="http://www.state.tn.us/tra/orders/2004/0400034dm.pdf">http://www.state.tn.us/tra/orders/2004/0400034dm.pdf</a>

TRA# 03-00491 F.C.C. T.R.O. Review - 03-00491

Testimony Address: <a href="http://www.state.tn.us/tra/orders/2003/0300491ib.pdf">http://www.state.tn.us/tra/orders/2003/0300491ib.pdf</a>

Rebuttal Address: <a href="http://www.state.tn.us/tra/orders/2003/0300491kn.pdf">http://www.state.tn.us/tra/orders/2003/0300491kn.pdf</a>

TRA# 03-00313 Petition of Nashville Gas to Adjust Rates

Testimony Address: <a href="http://www.state.tn.us/tra/orders/2003/0300313z.pdf">http://www.state.tn.us/tra/orders/2003/0300313z.pdf</a>

TRA# 03-00118 Petition of Tennessee American Water to Adjust Rates

Testimony Address: <a href="http://www.state.tn.us/tra/orders/2003/0300118bm.pdf">http://www.state.tn.us/tra/orders/2003/0300118bm.pdf</a>

Rebuttal Address: http://www.state.tn.us/tra/orders/2003/0300118ca.pdf

TRA# 01-00704 Audit of Atmos/U.C.G. IPA

Testimony Address: <a href="http://www.state.tn.us/tra/orders/2001/0100704cp.pdf">http://www.state.tn.us/tra/orders/2001/0100704cp.pdf</a>

TRA# 98-00559 BellSouth, C.S.A. Docket

Testimony is currently unavailable

TRA# 97-01364 United Cites Gas / Establishment of PBR

Testimony is currently unavailable

TRA# 97-01262 Permanent Prices

Testimony is currently unavailable

TRA# 97-00982 Petition of Chattanooga Gas to Revise Tariff

Copy Attached

### Before the

# TENNESSEE REGULATORY AUTHORITY

IN RE:
PETITION OF CHATTANOOGA GAS COMPANY TO PLACE INTO EFFECT A REVISED NATURAL GAS TARIFF
DOCKET NO. 97-00982
*****************************
DIRECT TESTIMONY
OF
STEVE BROWN
***

# TABLE OF CONTENTS

SUBJECT	PAGE
INTRODUCTION	1
OPINION ON EQUITY RATE OF RETURN	3
AGL IS THE APPROPRIATE COMPANY FOR COMPARISON	3
COMPARABLE COMPANIES	6
TESTS OF RECOMMENDED EQUITY RETURN	8
DISCUSSION OF MONTHLY COMPOUNDING	. 10
MORE EVIDENCE THAT AGL IS THE APPROPRIATE COMPANY FOR COMPARISON	16
DERIVATION OF DR. BROWN'S EQUITY RETURN: DCF ANALYSIS	18
DERIVATION OF EQUITY RETURN: RISK PREMIUM ANALYSIS	20
RISK PREMIUM MODEL: CURRENT COST OF DEBT	23
RISK PREMIUM MODEL: MARKET RETURN TO COMMON EQUITY	25
RISK PREMIUM MODEL: RISKFREE RATE	33
RISK PREMIUM MODEL: THE BETA	37
THE APPROPRIATE RETURN OF 10.55% COMPENSATES FOR MONTHLY COMPOUNDING	4 0

# TABLE OF CONTENTS (Cont.)

SUBJECT	PAGE
CAPITAL STRUCTURE AND OVERALL RATE OF RETURN	43
ANALYSIS OF METHODS EMPLOYED BY THE COMPANY'S COST OF CAPITAL WITNESS	45
SMALL COMPANY APPROACH IS IRRATIONAL	46
RETURNS OF 12.5% AND 12.17% ARE BASED ON LARGE COMPANY DATA, MISUSE OF DATA AND IRREGULAR, UNSUPPORTED PROCEDURES	52
DCF ANALYSIS IS BIASED UPWARDS	63
RANGE OF 11.5% TO 12.5% IS IRRATIONAL	64

#### INTRODUCTION

2

Q. Please state your name.

4 5

A. Stephen N. Brown.

6 7

Q. Where do you work and what is your job title?

8

10

A. I am a Senior Economist in the Consumer Advocate Division, Office of the Attorney General.

11 12 13

Q. What are your responsibilities as Senior Economist?

14 15 16

17

A. I review companies' petitions for rate changes and follow the economic conditions that affect the companies.

18 19 20

Q. What experience do you have regarding utilities?

212223

24

25

26

27

28 29

30 31

32 33

34 35

36

37

From 1986 to 1995 I was employed by the Iowa Α. Utilities Board as Chief of the Bureau of Energy Efficiency, Auditing and Research, and Utility Specialist and State Liaison Officer to the U.S. Nuclear Regulatory Commission. From 1984 to 1986 I worked for Houston Lighting & Power as Supervisor of Rate Design. From 1982 to 1984 I worked for Arizona Electric Power Cooperative as a Rate Analyst. From 1979 to 1982 I worked for Tri-State Generation and Transmission Association as Power Requirements Supervisor and Rate Specialist. From 1979 through 1995 my work spanned many issues including cost of service studies, rate design issues, telecommunications issues and matters related to the disposal of nuclear waste.

38 39 1 What is your educational background? Q. 2

3 Α. I have an M.S. in Regulatory Economics from the 4 University of Wyoming, an M.A. and Ph.D. in International Relations with a specialty in 5 6 International Economics from the University of 7 Denver, and a B.A. from Colorado State University. 9

8

Dr. Brown, have you authored any articles 10 0. 11 relating to your profession? 12

13 Α. Yes, my articles have appeared in Public 14 Utilities Fortnightly and the Electricity 15 Journal.

Are you and have you been a member of any Q. professional organizations, Dr. Brown?

- Α. Yes, I am a past member of the NARUC Staff Committee on Management Analysis, a past trustee of and a member of the Board for the Automatic Meter Reading Association, and a current member of the National Association of Business Economists.
- 27 Have you studied mathematics and statistics as Q. 28 part of your education? 29
- 30 Α. Yes. 31

16 17

18

19 20

21

22

23 24

25

26

32 Dr. Brown, do you use mathematics and Q. 33 statistics in combination with economics as 34 part of your profession? 35

36 Α. Yes. 37

38 Q. What were you asked to do with respect to this 1 case?

5

A. I was asked to form an opinion on the appropriate market-based common equity return, the appropriate overall cost of capital and the appropriate capital structure for Atlanta Gas Light (AGL) Company's wholly owned subsidiary in Tennessee, Chattanooga Gas (CG)Company, as well as to evaluate and assist in the evaluation of the rate of return proposed by other witnesses in this docket.

#### OPINION ON EQUITY RETURN

Q. In your opinion what rate of equity return is just and reasonable?

A. In my opinion an equity return of 10.55% is just and reasonable.

Q. Dr. Brown, what did you do to identify this just and reasonable return?

A. I examined a group of natural gas companies comparable to AGL.

# AGL IS THE APPROPRIATE COMPANY FOR COMPARISON

28 · 

Q. Why did you consider AGL the appropriate company for deriving the equity return?

A. CG's common equity is owned completely by AGL and is not publicly traded or available over the counter. Investors who desire a common equity interest in CG have only one way to obtain that interest—acquire common stock in AGL Resources, whose financial fate is determined by its prime subsidiary, AGL.

8 9

10 11 12

13 14

15

16

25 26 27

28 29 30

32 33

34 35

31

36 37

39

38

These facts alone suggest that AGL is central to the equity analysis. Also, in this docket AGL's management is well-represented. The company's witnesses -- Messrs. Thompson, Hinesley, and Overcast and Lisa Wooten -- are employed by AGL directly and none of them ever worked for CG directly. This is ample evidence that AGL management strongly directs CG's activities thus making AGL rather than CG the focus of equity analysis.

The direct involvement of AGL's management in this docket clearly indicates that CG's operations are completely intermingled with AGL's, to the point that CG is an operating company under AGL's management in much the same way that Savannah Gas is an operating company under AGL. When AGL has a rate case in Georgia, Savannah Gas is not singled out as a standalone investment of funds which forms the basis for a rate of return. Likewise, CG is not a stand-alone investment that forms the basis for a rate of return. The company's cost-ofcapital witness, Dr. Andrews, concedes this point very early in his testimony at page 4 lines 12-13, where he says "I undertake the analysis of CGC as if it were [emphasis added by Dr. Brown] a stand-alone investment of funds." To me, the wording "as if it were" means one of two things: either CG is not in fact a stand-alone investment or he does not know if it is a stand-alone investment.

Finally, Dr. Andrews, at page 48 lines 6-8 of his direct testimony, suggests the capital structure of AGL Resources be used to compute CG's weighted cost of capital. These aspects of the rate filing make it appropriate to

determine the cost of capital by using AGL and companies that are comparable to AGL.

Q. Does Dr. Andrews base his cost-of-capital analysis on AGL and companies comparable to AGL?

A. No, but his recommended return includes a premium meant to compensate AGL Resources.

Q. What companies form the basis for Dr. Andrews' cost-of-equity analysis?

A. He selects 22 "small" companies that have actively traded stock, that issue bonds and stocks, and which complete and file regular reports with the Securities and Exchange Commission. In contrast to CG, which is a subsidiary of AGL, many of the 22 companies are parent companies themselves with subsidiaries underneath them. Several of the 22 companies also operate in multi-state jurisdictions.

Q. In your opinion do these "small" companies are a rational basis for a cost-of-equity analysis in this docket?

A. No, I do not. On their face the 22 companies markedly differ from CG, and there is no objective basis for adjusting them so that they would somehow be comparable to CG. Because I focus on AGL, my cost-of-equity analysis uses a completely different set of companies than Dr. Andrews' analysis. A cost-of-equity analysis starts with the selection of comparable companies. To the extent the parties in this docket disagree about the starting point of an analysis, the TRA's job of assessing each

analysis becomes more difficult. However, I have other sound and objective reasons for disagreeing with Dr. Andrews' analysis and results, as I will discuss at a later point in my testimony.

### COMPARABLE COMPANIES SELECTED BY DR. BROWN

# Q. Dr. Brown, what comparable companies did you use in your analysis?

 A. I selected a group of companies composed of AGL Resources, Bay State Gas Company, Brooklyn Union Gas Company, Indiana Energy, Laclede Gas, Northwest Natural Gas, Peoples Energy, and Washington Gas Light Company. Like AGL, all of these companies have subsidiaries.

Q. What evidence do you offer to substantiate your assertion that AGL is comparable to the other eight companies?

21- --

The proof of comparability appears in Schedule Α. 1. The top portion is titled "Market Statistics" and the bottom portion is titled "Financial Behavior." The market statistics show the strong similarity of the companies. For example, as of December 1996 the ratios of the market price to the book value are similar, and so are the equity ratios, dividend yields, the value of the holdings per shareholder and the average number of years the stock is held. However, the market values have a large spread. The smallest value, \$343 million, is about only one-fourth of the largest market value.

Q. Dr. Brown, is the difference in market values of the comparables you selected meaningful?

37 A. 1

A. No. My examination of the companies shows that they exhibit similar financial behavior, as indicated by the way they responded to the publication Value Line's criticism of the gas distribution industry. That criticism is quoted in Schedule 1. In early 1995 Value Line warned investors to be wary of gas companies that paid out more than 80% of their earnings to dividends. Prior to Value Line's warning many payout ratios exceeded 80%. From 1995 to 1996, however, every company lowered its payout ratio to levels below 80%. This deliberate response by all the companies makes it clear that they have comparable financial behavior.

- Q. Is your opinion of the equity return different from the equity return recommended by Dr. Andrews?
- A. Yes, he recommends a higher, speculative range of 11.5% to 12.5% and prefers 12.25%, a much higher, speculative rate.
- Q. Upon what do you base your equity return opinion?
- A. I base my opinion on my analysis of AGL's market-based cost of common equity, which is supported by my analysis of comparable companies.
- Q. In your opinion what rate of equity return should the Tennessee Regulatory Authority allow in this docket?
- A. My opinion is that the Tennessee Regulatory Authority (TRA) adopt the equity return of

1 10.55%.

2

# TESTS OF RECOMMENDED EQUITY RETURN

4 5 6

# Q. Dr. Brown, did you compare your equity return to those of independent sources?

7 8 9

10

11

12 13

14

15 16

17

18 19

20

2.1

Yes. Chart One summarizes the tests I made. I Α. compared my results to the information published by Merrill Lynch regarding the required rates of return for gas distribution companies in general. I also compared my results with the equity returns recently granted by the Illinois Commerce Commission and the Virginia State Corporation Commission to United Cities, a company currently under the TRA's jurisdiction and one that is included in Dr. Andrews' analysis. The Merrill Lynch returns are shown in Schedule 2. Press releases announcing the Illinois and Virginia decisions are attached as Schedules 3 and 4 respectively.

2223

24

25

Q. What was your reason for using Merrill Lynch's data?

26 27

28 29

30 31

32

33

34

35

A. Merrill Lynch's data reflects the marketplace for gas distribution companies, and I have used their data as a basis of comparison in prior rate cases. From January 1995 through May 1997 Merrill Lynch's equity-return estimates have ranged from a high of 11% to a low of about 9%. My recommendation of 10.55% approximates Merrill Lynch's upper limit of recent equity returns for the natural gas distribution industry.

36 37 38

39

Q. What was your reason for comparing the recent equity awards by two state commissions?

A. My reason for comparison was to consider independent sources. The comparison merely demonstrates that my recommended return is consistent with recent regulatory decisions regarding equity returns in other jurisdictions.

9 Q. Did you compare the data from Merrill Lynch and 10 from the various states to Dr. Andrews' recommended return to equity?

A. Yes. Dr. Andrews' recommended return substantially exceeds any reasonable return for the industry, and therefore is more than just and reasonable.

Q. Dr. Brown, is the return you are presenting a fair return?

A. Yes. It is a fair return because it compensates the company for ordinary financial risks it is taking to be in the gas distribution business.

Q. What are the sources of ordinary financial risk to the company?

A. The major risk is that the company's expenses would increase faster than its revenues. However, in this case that risk is negligible. The company's rate base, expenses, and sales are based on projected amounts for a 12-month period ending September 1998. These factors are the basis for the prices that come out of this docket. However, the company's prices are likely to be applied almost a full year before the projections are realized.

For there to be any risk, the company's projected expenses would have to be far less than what actually occurs, or the company's projected sales of gas would have to very different from the actual sales. I know of no substantial evidence suggesting that the company's forecasts will create a financial hardship.

Q. Dr. Brown, is your rate of return sufficiently high to allow the company to attract capital and to maintain creditworthiness?

A. Yes. An annual return of 10.55% is certainly high enough to attract capital and to maintain creditworthiness. The rate-of-return principles of capital attraction and maintenance of credit were set in the *Bluefield* decision, and the rate of return I recommend considers these factors.

 Also, 10.55% is an understatement of the amount that the company actually has an opportunity to earn because the actual annual return is achieved through monthly compounding, which raise the return by approximately one-half a percent to 11%.

# DISCUSSION OF MONTHLY COMPOUNDING

Q. Is the monthly compounding process typical of the financial world?

A. Yes.

Q. Do monthly earnings have to be constant for monthly compounding to operate?

19

20 21

22

23

24 25

26

27

28 29 30

39

- No. Schedule 6 shows that compounding occurs with income-losses and with income-gains. The Schedule is based on the actual monthly income and losses of AGL for the fiscal year 1996. The far right-hand column clearly shows that monthly compounding of \$1 at an allowed annual return of 10.55% leads to an effective return of 11.0%. With regard to column (6), at the bottom, the total return is shown as 11.02 cents. The total return would equal 10.55 cents only if the monthly return in column (6) is not added into the cumulative balances in columns (5) and (7), i.e., the cumulative balance would have to be \$1 throughout the entire year. But this is not how financial processes work cumulative balances are maintained on a monthly basis and changes to the balances are recorded monthly - not just annually.
- Dr. Brown, are you this docket's only cost-of-Q. capital witness who believes that compounding is a typical financial process?
- No. Dr. Andrews has made several statements indicating his opinion that compounding is a typical financial process:

Dr. Andrews, in his direct 31 testimony page 27, line 5 says 32 that "financial processes 33 occur continuously." 34 Therefore, his discounted cash 35 flow (DCF) analysis is 36 predicated on dividends 37 continuously compounding, 38

1.

indicated at page 26 line 18 of his testimony, a situation

36 37

38

39

ζ.

where compounding goes on moment-by-moment, a far more rapid rate of compounding than a monthly rate.

- 2. Dr. Andrews' direct testimony, page 28, lines 15-17, suggests that compounding a return of 9.53% leads to an effective return of 10%, clearly indicating that compounding adds approximately one-half percent to the return. This is the same point that I have made about compounding.
- 3. Dr. Andrews was cross-examined in Docket 95-02116 and stated that "Financial processes occur smoothly and continuously. They go -- if this makes the point for you -- minute by minute, hour by hour, day by day and they are not interruptible." His statement occurs at page 8, lines 20-23 of the transcript. A copy of the transcript's cover page and page 8 of the transcript are attached to my testimony as Schedule 7, pages 1 and 2 respectively.
- 4. His statements under crossexamination are consistent with his direct testimony page 28 lines 10-11, where the question is asked if there is "complete equivalency between

the continuous" rate, such as 9.53%, and a so-called "finite" rate, such as 10%. He answers "Yes."

5. His responses in his deposition of September 9 are also consistent with his testimony. For example, at page 58 line 16 of the deposition he was asked how often compounding occurred:

"Q. Right, and it doesn't even have to be a series of years, it can be series of months, can't it?"

To which Dr. Andrews responded:

"A. It could be done months, weeks, days."

He was also asked in the deposition, at page 59 line 10, whether he concurred that compounding is typical of financial processes:

"Q. ...compounding is essentially accepted by all of our financial markets?"

To which he responded:

"A. Sure."

# Q. What does the term "compounding" mean?

A. The term compounding refers to a process that begins with a certain financial resource, generally called the base or the principal, and then the changes in that are added back into the base or the principal to create a new balance. The changes can be either positive or negative, meaning that the principal is either growing or declining.

Two things affect compounding.

The time-frame of compounding -- how quickly is the change added back to the base? It could occur once a decade, once a year, once a month, every day or every second.

The size of the change during the time frame -- does the base change by 1% a month each month or does it change by 2% in some months and 3% in other months?

 The financial community puts these concepts together to say things like "your investment is growing at a rate of 10% per year this year, but last year it lost money at annual rate of 3%." Therefore, compounding describes financial gains as well as financial losses and does not have to occur at the same rate from one moment to the next.

Q. Is compounding process related to concept of working capital?

A. No. Working capital encompasses only the funds

needed by the company to meet its current liability, i.e., the company has to have the funds available to meet its demands for cash flows.

4 5 6

7

1

2

3

# Q. Why are you referring to working capital?

A. I raise it now to assure the TRA does not view monthly compounding as akin to working capital, where positive and negative cashflows are balanced by short-term lending and short-term borrowing.

13 14

15

16 17 Q. Is monthly compounding an accurate description of how a distribution company accumulates annual return even when the company experiences seasonal variations in sales, revenues and expenses?

18 19 20

21

22

23

2425

26

2728

29

30

31

32

33 34

35

36 37

38 39 A. Yes. The returns in the months when sales are high balance the returns in the months when sale are low. This is true whether the annual return is viewed as a sum of compounded monthly returns or as just the sum of twelve monthly returns that are not compounded. However, monthly compounding reflects the true nature of financial transactions. Revenues flow in every working day and are available for immediate reinvestment. The company's stocks and bonds can be bought and sold every working day of the year. The best indication that the compounding process underlies the company's financial transactions is the company's late fee, which applied to consumers' monthly bills if they are not paid by the past due date. The late fee truly shows that "time is money." The quicker the company has the money, the quicker it can be invested to achieve additional returns. This is a perfect fit with the monthly compounding

cycle that typifies financial transactions in our economy. If monthly compounding were not how a gas company accumulated its annual return, there would be no economic basis for charging a late fee.

Q. When Dr. Andrews' recommended equity return of 12.25% is compounded monthly, what return is the company being given an opportunity to earn?

A. The company is being given an opportunity to earn about 12.8%

# MORE EVIDENCE THAT AGL IS THE APPROPRIATE COMPANY FOR COMPARISON

Q. If Dr. Andrews' recommended return of 12.25% a just and reasonable return?

A. No. His preference for 12.25% is meant to compensate AGL Resources (the parent of AGL) for the premium the company paid when it purchased CG. At page 3, lines 5-8 of his testimony Dr. Andrews states. "The point estimate is slightly off center in an upward direction in recognition of AGL Resources' long-run inability to earn on a rate base that includes the acquisition premium it paid as part of the price for CGC."

Q. What inferences do you make from Dr. Andrews' statement?

A. The statement confirms that this rate case is about AGL's return and that AGL and companies comparable to AGL should form the basis for an equity analysis. Dr. Andrews' statement also contradicts his later statement at page 4 lines

9-10 where he states: "the source of an investment's financing does not dictate its fair rate of return." His recommendation of 12.25% clearly aims at achieving a return for AGL, the owner of CG.

Q. Is Dr. Andrews choice of 12.25% as his preferred return consistent with his statement: "I treat CGC as if it were a stand-alone investment of funds?"

13、 

A. No. If CG were a stand-alone investment there would be no reason for Dr. Andrews to consider the acquisition premium as a factor or justification for choosing 12.25%. This justification is Dr. Andrews' tacit recognition that CG is not a stand-alone investment.

21 .

Q. How does Dr. Andrews' supposition of CG as a "stand-alone" investment compare with the testimony of other witnesses for AGL?

A. His supposition is contrary to the facts presented by Mr. Thompson, whose direct testimony, pages 11 through 22, describes the various support services that AGL provides to CG. For example, at page 17 line 6 Mr. Thompson lists several functions provided by AGL. At page 16 lines 4-15 Mr. Thompson indicates that AGL's Treasury and Corporate Accounting departments handle many transactions for CG. At lines 7-8 he says, "All checks for Chattanooga Gas Company are written by AGL." At page 13 line 11 he describes the various departments that have been eliminated at CG.

Q. Do you agree with Dr. Andrews' testimony, at page 6 line 8, that CG has "sharply expanded

### demands for financing."

 A. No. His statement is contradicted by the capital structure information the company supplied in this docket and in its prior rate case. In docket 95-02116, the company submitted a capital structure of \$96.846 million. That structure is attached to my testimony as Schedule 8. In the current docket the company submitted a capital structure of \$95.843 million, shown in the company's filing as Exhibit 5 Schedule 9. AGL is withdrawing its investment from Tennessee rather than suffering from a sharply expanded demand for financing

Q. What is the implication of the \$1 million decline regarding CG as a "stand-alone investment?"

A. If a stand-alone company's capital dropped by \$1 million, there would be an accounting trail, but in this instance there is no trail at all for CG. Therefore, the \$1 million difference has to be the result of AGL's decisions and way it adds and subtracts funds to its Tennessee operations.

# DERIVATION OF DR. BROWN'S EQUITY RETURN: DCF ANALYSIS

Q. Did you perform an analysis to determine what the return to equity should be for AGL's wholly owned subsidiary?

A. Yes. I performed two analyses: one based on the Discounted Cash Flow (DCF) model and another based on the risk premium model.

## Q. What is the Discounted Cash Flow model?

A. The DCF model is a standard way that investors evaluate their potential returns. The model defines the cost of common equity as the dividend yield plus the dividend's expected growth rate.

5

# Q. What is the advantage of using the DCF model?

A. It does exactly what every investor does. It pays close attention to the company's dividend per share of common stock and to the company's ability to raise or lower the dividend and the dividend yield.

## Q. What is the dividend yield?

A. Dividend yield is measured as the company's annual dividend divided by the price for the company's stock. I've used the average dividend yield of the comparable companies as a proxy for AGL's dividend yield. The calculations are shown in my Schedule 9. In this instance the calculated dividend yield is 5.17%.

# Q. What did you use to measure dividend growth?

 A. Since AGL's current dividend growth rate is barely above zero, I used the growth rate derived from Value Line's projection of AGL's dividend in the year 2000, which suggests a growth rate of 5.23% in the near future. Thus my estimated DCF equity return is 10.40%, shown in Schedule 9.

Q. Does the DCF Model account for capital gains that may occur when an investor sells stock?

No. The DCF model avoids entanglement with Α. either capital gain or capital loss because the model is tied directly to dividend yield and dividend growth. In addition, losses and gains are a matter of the investor timing the stock's purchase and sale. The DCF model neither protects investors from risk nor penalizes them for what happens in the stock market.

8 9

1

2

3

4

5 6

7

10

### 11 12

#### 13 14

15

16 17

18 19

20

21. 22

23

24

25 26

27

28

29 30

31 32 33

> 34 35

36

Q. 37

38 Α. DERIVATION OF EQUITY RETURN: RISK PREMIUM ANALYSIS

- In addition to your DCF model, did you use Q. another method to determine the market based cost of common equity?
- Yes. I used the risk premium method which Α. defines the cost of equity as the market's current debt yield plus an estimated risk premium. For example, a current debt yield of 7% plus an estimated market wide risk premium of 3% produces an estimated common equity cost of 10%.
- Is a risk premium analysis different from a DCF Q. analysis?
- Yes, the two analyses are completely different. Α. For example, dividend growth and dividend yield are crucial to the DCF analysis, but they have no role whatsoever in a risk premium analysis.
- What is the rationale of risk premium analysis?
- Investors require extra payments to assume

additional risk. Economists call this extra payment a risk premium. Equity investments are riskier than debt because equity investments occasionally lose money, thus equity investors require a risk premium or a higher return than debt. For example, equity holders are last in line for the distribution of earnings and also last in line for distribution of liquidation proceeds. In both cases the debt holders are paid first. Any funds left are distributed to the equity holders. Therefore, the cost of equity is the debt yield plus a risk premium for the company.

#### Q. How did you derive your risk premium model?

A. The model is derived as follows:

$$K_e = R_f + (R_m - R_f) * B_e$$
 (1)

 K<sub>e</sub> is the cost of equity

23 K<sub>e</sub>

where

 $\mathbf{R}_{\mathbf{m}}$  is the market rate of return

 $R_{\mbox{\scriptsize f}}$  is the risk free rate of return

 ${\rm B_{\rm e}}$  is the beta for common stock

31 and

$$K_d = R_f + (R_m - R_f) * B_d$$
 (2)

where

 $K_d$  is the cost of debt

 $\mathbf{R}_{\mathrm{m}}$  and  $\mathbf{R}_{\mathrm{f}}$  are defined above

 $B_{\rm d}$  is the beta for debt

Subtract equation (2) from equation (1) and the result is

$$K_e = K_d + (R_m - R_f) * (B_e - B_d)$$

I treat the beta for debt,  $B_d$ , as if it were zero. Since  $B_d$  is zero, this raises the cost of common equity that can be derived from this model. Since  $B_d$  is zero, the final result is

$$K_e = K_d + (R_m - R_f) * (B_e)$$
 (3)

- Q. What is the procedure for deriving the cost of equity from this risk premium model?
- A. The procedure has six steps:
  - Estimate the market's current cost of debt - K<sub>d</sub>.
  - 2. Estimate market-wide rate of return for common equity  $-R_m$ .
  - 3. Estimate the market-wide risk-free investment  $R_f$ .
  - 4. Take the difference between steps 2 and 3
  - 5. Multiply the difference by a so-called "Beta"  $B_e$ .
  - 6. Add the result of step 5 to the debt cost in step 1. The result is the estimated cost

of equity from the risk premium model
3

#### RISK PREMIUM MODEL: CURRENT COST OF DEBT

Q. What do you use as the current cost of debt -  $K_d$ ?

A. Since AGL's bonds retain an A rating, I use the monthly average of A-rated bonds for May 1996 through April 1997. Those are shown in Schedule 10 and represent the current trend in capital cost for debt issues of A-rated utility bonds.

Q. What is the value of the K<sub>d</sub>?

A. The value of  $K_d$  is 7.95%.

Q. Are the A-rated bonds long-term bonds?

A. Not necessarily. For example, the source for this information is the Federal Reserve Board which says these bonds have a maturity of 30 years but call-protection for only 5 years, i.e, after 5 years and depending on the issuing company's discretion, the bonds can be repurchased from the investor.

Q. Is it typical for companies to have call provisions in their bonds?

A. Yes.

37 Q. What is the purpose of a call provision?

- It gives the company control and flexibility 1 Α. 2 regarding the disposition of its funds and transfers the risk of interest rate changes 3 4 from the company to the investor. For example, if a company issues bonds at 10% and six years 5 6 later interest rates drop to 7%, the company 7 has the option of "calling" the bond from the 8 investor, who then has to find an alternative 9 use for the funds. Continuing with this example, if the company issues bonds at 7% and 10 six years later interest rates rise to 10%, the 11 company has no need to repurchase the bond from 12 13 the investor, who has the choice of either 14 holding the bond or taking a loss in principal 15 if it is sold. 16
  - Q. Why do you use the A rates as a measure of debt cost instead of AGL's embedded debt cost?

18

19

37 38

39

- 20 Risk premium analysis is based on market wide indicators of current debt cost instead of a 21 ... company-specific embedded cost. Using a 22 23 company-specific embedded cost would mean that the company with the highest debt cost would 24 25 also receive the highest return to equity. 26 Conversely, the company with the lowest debt cost would receive the lowest return to equity. 27 28 Thus using a company-specific debt cost to establish a risk premium would introduce 29 incentives for companies to raise their debt 30 31 cost as much as possible. That is unreasonable logic and unreasonable financial management. 32 33 Fortunately, the markets don't work that way. A 34 company's return to equity is not guaranteed to be a certain amount higher than the company's 35 36 debt cost.
  - Q. Why do you use the A bond rates as a measure of debt cost instead of the average debt cost of

#### the comparable companies?

A. The company average would not necessarily reflect current market rates for bonds rated as A, the current rating for AGL's bonds.

, 

#### RISK PREMIUM MODEL: MARKET RETURN TO COMMON EQUITY

# Q. What do you use to estimate $R_m$ , market-wide rate of return for common equity?

A. I use 10.7%, the compound annual growth rate for large company stocks from the period 1925-through 1996. This figure is taken from Ibbotson Associates 1997 Yearbook- Stocks Bonds, Bills and Inflation (SBBI-1997) page 118.

## Q. Why are using large company stocks?

A. The comparable companies that I use in my analysis fit into the large company category, defined in SBBI-1997 page 136 as any company exceeding \$197.4 million in market value as of September 1996. The smallest market value for my comparable companies is \$343 million.

# Q. Why are you using historical data to estimate the risk premium?

A. Historical data provides a way to smooth out the wild fluctuations in the risk premium, which is the difference between the risk-free return and market return to common equity. Since return to debt is fairly stable, the

fluctuations are caused by the wide swings in the return to equity. For example, if the return to common equity is large in one year, so is the premium, if the return is small the next year, the premium will be negative.

6 7

# Q. Why are you using the years from 1925 through 1996 to measure the risk premium?

8 9 10

11 12

13 14

15

16

17

18

19

20

21

22

23

2425

26

27

28

Ibbotson provides historical information on the risk premium from 1925 through 1996, and these years represent the entire term for which information is available. Using the entire data avoids any element of subjectivity that may influence the selection of only a portion of the data. Neither Ibbotson nor anyone else I know of recommends using just a portion of the data. SBBI-1997 discusses this issue at pages 152-153: "A proper estimate of the expected risk premium requires a long data series, long enough to give a reliable average without being unduly influenced by very good and very good and very poor short term returns ... More generally, the 71 year period starting with 1926 is representative of what can happen. SBBI-97 also warns: "Some analysts calculate the expected equity risk premium over a shorter, more recent time period...this view is suspect."

29 30 31

Q. Why are you using 10.7% as the estimate of the market-wide rate of return to common equity?

33 34

35

32

A. I use that figure because it represents normal performance in the market. I have two reasons for saying so.

36 37 38

39

The first reason is a plain and simple one: 10.7% is the actual compound rate of growth in

the value of large companies' common stocks. SBBI-1997, at page 49 states: "One dollar invested in large company stocks at year end 1925, with dividends reinvested, grew to \$1370.95 by year end 1996; this represents a compound annual growth rate of 10.7 percent." The year-by-year change in the large companies' value is shown in Schedule 11 column (2).

10 The second reason is also simple. Not all large 11 companies' stocks have advanced at a compound 12 rate 10.7%. Some companies have earned more 13 than 10.7% and others have earned less. In the 14 71 year period covered by data, there are 15 literally millions of possible outcomes. But 16 out of the millions of possibilities, the 17 number of possibilities below 10.7% are exactly 18 equal to the number of possibilities above 19 10.7%. Thus 10.7% is the exact middle of all 20 the possibilities that could have occurred.

> is a 50% chance that the compound return will be 10.7% and a 50% chance that a \$1 investment in 1925 would be worth \$1370.95 in 1996. Returns higher than 10.7% have a smaller chance

This idea may be expressed another way: there

Returns higher than 10.7% have a smaller chance of being achieved.

272829

30

31

21

22

23

24

25

26

1 2

3

4

5

6

7

8

9

Schedule 12 and Charts 2 and 3 show the exact odds of achieving 10.7% versus the other possibilities.

32 33

## Q. How did you derive Schedule 12?

34 35

36

37

38

39

A. I have provided the mathematical details in Appendix A. But the heart of the concept is simple. A \$1 investment today has two possible outcomes next year -- a gain or a loss. But in the year after next, there are four

possibilities because each possibility in the first year has two possibilities in the second year. The number of possibilities doubles each year. Thus an investment that begins with \$1 has 8 possible values three years later, 16 possible values four years later and so forth. The SBBI-97 data on large companies covers seventy one years and literally millions of possibilities. But the odds of each possibility can be easily calculated. I have done that in Schedule 12.

# Q. Why have you highlighted certain portions of Schedule 12 and Charts 2 and 3?

A. I highlighted those portions to show the tieins of the schedule and the charts back to
Schedule 11 and to emphasize the difference
between the actual rate of 10.7%, which appears
at the bottom of column (2) in Schedule 11 and
the figure of 12.7%, which appears at the
bottom of column (3), the so-called average of
the returns, which I describe as a "biased
average."

# Q. Why do you consider the average to be biased?

 A. The average is biased in the sense that it overstates market returns and leads unwary investors into the mistaken notion that an "average" return has a 50% chance of being achieved, when it does not. The growth rate of 12.7% means that a \$1 investment in 1925 is now worth \$4768 instead of \$1371. Thus the rate of 12.7% is biased.

The bias is created in a very simple way: No one can ever lose more than 100% of their investment, i.e., 100% is the mathematical limit for losses. However, there is no mathematical limit for an investment's gain. Therefore, when percentage gains are combined with percentage losses the resulting average is mathematically biased to overstate the true gain in value. An excellent example is provided by Roger Ibbotson, the principal of Ibbotson Associates and the author of SBBI-97. July-August 1979 issue of Financial Analysts Journal, at page 44, he wrote::

"Suppose that \$1.00 were invested in a common stock portfolio that experienced 100 percent price appreciation in the first year and 50 percent depreciation in the succeeding year. At the end of the first year the portfolio would be worth \$2.00; at the end of the second year the portfolio would be \$1.00. The [average]...return on the portfolio would be 25 percent

By adding a gain of +100% to a loss of -50%, the net is +50% and the average is 25%. Since the portfolio's value is again \$1.00, the actual return is obviously zero, not 25%. Thus, the "average return" is clearly a biased and misleading estimate of the return to equity. This example also shows that the actual return is computed by comparing numbers that represent actual values rather than by averaging numbers expressed as rates of return.

Q. Is there any situation in which the average return is not biased?

9

10

11

12 13

14 15

16 17

18 19

20 21

22 23

24 25

26

27 28

29

30 31 32

34 35

33

36 37

38

Yes. If the market always gains, then the Α. average is not biased. In this situation the average return and the actual return are identical. A divergence between the actual return and the average return indicates that losses have occurred. The greater the divergence, the greater the losses in the market.

Is 10.7% derived by comparing two actual Q. values?

- Yes, it is derived by comparing the market Α. value of large companies' common stock in 1925 with the their value in 1996, which I show in Schedule 11.
- Is 12.7%, the biased average in your terms, derived by averaging numbers expressed as rates of return?
- Yes, it is derived by averaging all the rates A. of return from 1925 through 1996.
- Does the figure 12.7% result from the Q. mathematical bias you described?
- Yes because there have been several years where Α. the market lost value. This is indicated in Schedule 11 column (2) when the value for an earlier year is greater than the value of a later year. For example, the market index fell from 534.46 in 1989 to 517.5 in 1990.
- What are the odds of a company achieving at Q. least a 12.7% return?

1 A. The odds are less than 1 in 5 or less than 20%, indicating the return represents superior performance rather than normal performance.

**4** 5

Q. What are the odds of a company achieving at least a 10.7% return?

6 7 8

9

A. The odds are 1 in 2 or 50%, indicating that the return represents normal performance.

10 11

12

Q. Why have you made the effort to explain the differences underlying 10.7% and 12.7%?

13 14

15

16

17 18

19

20

21

22 23

24

25

26 27

28

29

30

31

Market returns vary widely over time, and when Α. people are confronted with extremes the first step in clarifying the situation is to take an average. But with regard to a rate of return, it is a mistake to assume that an average is the mid-point between the extremes and that the average represents a typical value. I want to. make this fact clear. In addition, I have not seen any direct testimony presented to the TRA or its predecessor agency where the differences are explained in terms of probability. Without a probability analysis the difference between 10.7% and 12.7% may seem tiny and unimportant. However, when the probability of achieving 12.7% is considered, it is clear that 12.7% is a return representing superior performance in the market rather than normal performance. Thus 12.7% is not a rational basis to set a risk premium rate.

32 33

34

Q. Is it reasonable to describe the risk premium in terms of a probability analysis?

35 36 37

38

39

A. Yes. SBBI-97 at page 155 states: "in the investment markets...returns are described by a probability distribution..."

- 1 Q. Is the return of 10.7% certain to be achieved?
- A. No, there is a 50% chance that it will not be achieved.

7

8

17

18 19 20

21

222324

25

26

Q. Is there disagreement about whether a risk premium should be derived from 10.7% or 12.7%?

- 9 Yes. The disagreement is generally discussed in Α. terms of a debate about the merits of using the 10 11 "geometric mean" of market returns versus using the "arithmetic mean" of market returns. The 12 10.7% figure is the geometric mean of large 13 companies' historical returns, and 12.7% is the 14 15 arithmetic mean. 16
  - Q. Are you using the geometric mean or the arithmetic mean in your risk premium analysis?
    - A. I use the geometric mean, but I prefer the phrase "actual return." I prefer to call the arithmetic return the "average return."
    - Q. Do you have support for your choice of the geometric mean over the arithmetic mean?
- 27 Yes. In addition to the all the reasons I have Α. already described for using the geometric mean, 28 it is also preferred by scholars in statistics 29 30 and finance as well as professional investment 31 firms. In 1990, Thomas Copeland, et. al. published Valuation: Measuring and Managing the 32 Value of Companies. At page 193 they state: 33 "Our opinion is that the best forecast of the 34 35 risk premium is its long run geometric 36 average." Irving Fisher, considered to be one of the world's greatest statisticians, wrote a 37 book called The Making of Index Numbers. In the 38

1967 edition of the book at pages 29 and 30 Fisher says, "The simple arithmetic average produces one of the very worst index numbers. And if this book has no other effect than to lead to the total abandonment of the simple arithmetic type of index number, it will have served a useful purpose." In 1981 Richard Stevenson and Edward Jennings published, Fundamentals of Investment 2sd ed. At page 272 they say, "Why not simply average the rates of return? Indeed, in certain instances, such a procedure would be satisfactory. However, such an average would generally be meaningless." On March 13, 1990 at page C1 the Wall Street Journal ran the following story, "When Figuring the Rate of Return Don't Be Confused By The Sales Hype." The story compares the average return with the so-called compound return, another common name for the geometric return. The WSJ story says the compound return is "more widely used by investment firms."

22 23

There is plenty of support for using the actual market return (the geometric mean) in the risk premium model.

25 26 27

24

#### Q. What portions of the risk premium model have you identified thus far?

28 29 30

31

32

33

A. I have identified the debt and equity portions. In terms of the model --  $K_e = K_d + (R_m - R_f) * (B_e)$  --I thus far identified  $K_d$  as 7.95% and  $R_m$  as 10.7%. I still have to identify  $R_f$ , the risk free return and  $B_e$ , the beta.

34 35 36

RISK PREMIUM MODEL: RISKFREE RATE

38 39

37

Q. What represents the market-wide risk-free investment, R<sub>f</sub>?

 A. In this case I am using the three-month U.S. Treasury bills. I will show that the three-month rate is based on a long term perspective of the riskless rate and that it is a better concept to use in this case than a long-term bond.

Q. What is the market-wide risk free rate of return,  $R_{f}$ , based on three-month bills?

A. The risk free rate is 3.7%, which is the compound annual growth rate in the value of the three-month treasury bills from 1926 to 1996. Schedule 13 shows the 71 year history for returns to Treasury bills, and in the entire time there is no loss. The compound rate of 3.7% is the center of all possible outcomes from a \$1 investment in three-month bills in 1925. The average rate is 3.8%. It is slightly higher than the actual rate because there were no gains in several years. The three-month rate is the best measure of a riskless rate.

Q. Why is the three-month treasury bill the best measure of a riskless rate?

A. There are three reasons:

1. The three-month bill is a debt instrument. This fits with the risk premium's basic premise: the return to debt is less than the equity return and equity return is determined by referencing debt.

2. Of all the other debt instruments

measures that could be used -- long-1 2 term corporate bonds, long-term 3 government bonds, the income portion 4 of long-term government bonds and 5 intermediate term government bonds --6 the three-month bill provides the 7 lowest rate. This is consistent with 8 the financial concept that a risk free 9 rate should be lower than rates that 10 reflect risk.

11 12

13

14

15

16

17

18

19

20

21 22

23

24

25

26

27

28

29

30

A three-month bill is free from losses 3. but the other debt instruments are not, i.e., they are riskier forms of investment than the three-month bill, which is why their rates are higher. Schedule 14 shows the actual return and the average return 1925 to 1996 for each of the debt instruments. For each kind of debt, the difference between columns (2) and (3) indicates the degree to which the losses occur in that particular debt market. Of all the debt instruments, the three-month bill is the safest. Investors are absolutely certain of what cash flows will be received and when they will be received. Unlike the other debt instruments, the three-month bill carries no risk of default or loss of principal.

31 32 33

34

35

Q. Is there a contradiction between using the three-month bill as the risk free rate while you are using the cost of A rated bonds in your model?

36 37 38

39

A. No. I have already said those bonds are not necessarily long-term notes. They have call

provisions that transfer the risk of interest rate changes from the company to the investor. The three-month bill allows the investor to do the same thing the company does: avoid the risk of interest-rate changes.

6 7

#### Q. Is there a way to avoid the risk of losing principal and still use long term bonds?

8 9 10

11

12

13 14

15

16

A. No. SBBI-97 at page 151 suggests that long-term bonds have so-called "income returns." This return is the income an investor would receive if the bond were purchased and held to maturity rather than selling it. SBBI-97 considers the income return to be the "riskless portion" of an investment in long term bonds. I disagree with this concept because it is irrational.

17 18 19

20

21

#### Q. Why is the concept irrational?

30

31

32 33

34

35

36

37

38 39

It is irrational because it assumes an investor Α. can divide a long term bond into a riskless portion and a risky portion. This separation is not credible because a bond is not severable into distinct portions. The purchase of a long term bond always carries the risk that changes in interest rates will cause a change in the bond's value. The concept of "income returns" also suggests that once a long term bond is purchased, the investor will take no action until the bond matures and do nothing in the face of interest rate changes. This behavior is just the opposite of the behavior assumed in a call provision, which gives the issuer the flexibility to act when interest rates change. It is irrational to assume that the issuer of a bond is free to respond to interest rate changes but that the bond's buyer is not.

- Q. What portions of the risk premium model have you identified thus far?
- A. In terms of the model --  $K_e = K_d + (R_m R_f) * (B_e)$  \_- I have identified  $K_d$  as 7.95%,  $R_m$  as 10.7% and  $R_f$  as 3.7%. The term  $(R_m R_f)$  is equal to 7%. This amount would be smaller, as would my recommended rate of return, if I were to use any debt instrument other than the three-month bill. For example, if I were to use long-term government bonds, the term  $(R_m R_f)$  would be (10.7% 5.1%), which equals 5.6%. This lowers the risk premium equity return by 1.4%, which is the difference between 7% and 5.6%. I still have to identify  $B_e$ , the beta.

#### RISK PREMIUM MODEL: THE BETA

#### Q. What does beta measure?

、8 

A. Beta measures how an individual company's market value changes relative to the change in the value of the entire market. For example, if a company's market value increases from \$10 to \$11, then the company's value increases by 10%. If the entire market's value increased from \$1000 to \$1200, then the entire market's value increases by 20%. The beta is calculated as .5, which is the ratio of 10% divided by 20%.

The market itself has a beta of 1. If the company's beta is one, then the company risk premium is the same as the market-wide risk premium. Thus if a company's beta is less than 1, then the company is judged less risky than the market. Beta is also used to compare the relative riskiness. For example, a beta of 0.4

1 is less risky than a beta of 0.6. 2

3 4

#### Did you calculate betas for AGL and the Q. comparable companies?

5 6

7

8

9

10

11

12

Yes, and I also calculated the betas' accuracy. Α. The betas and their tests of statistical accuracy, the T-statistic, appear in Schedule 15, pages 1 and 2 respectively. The average beta shown at the bottom of page 1 Schedule 15 is transferred to Schedule 16, which provides results of the risk premium analysis.

13 14

Q. What is the beta's value in your model?

15

The value is .458 and is shown in Schedule 16 16 Α. 17 at the bottom of column (b).

18

19 What is the estimated equity rate of return Q. that is derived from your risk premium model? 20 21 .\_

22 The model gives a value of 11.14%. In terms of Α. 23 the model --  $K_e = K_d + (R_m - R_f) * (B_e)$  -- the 24 equity return is 11.14% = 7.95 + (10.7%-25 3.7%) \* .458.

26 27

Do you use all the betas in Schedule 15 to Q. develop the figure of .458?

28 29 30

Yes. I used the average betas that have an average Α. T-statistic greater than 1.

31 32

33 Why did you use the T-statistic and T-statistic Q. 34 greater than 1?

35

In general, the T-statistic indicates how well 36 Α. a summary number represents the group from 37 which the summary number comes. 38 In this case

the summary number is a beta, which few people are familiar with. But the T-statistic can also be explained in terms of an average, a summary number which everyone uses almost everyday.

5 6

7

8

10 11

12

13

14 15

16

17

18 19

20 21

22

23

2425

26

27

For example, I may know that a certain group of people are, on average, 40 years old. But the average is just a short-hand description of the group. The average alone does not indicate anything about the group's composition. The group could be composed of children younger than 10 and elderly people over 70. The group as a whole just happens to have an average age of 40 even though 40 is not at all representative of anyone in the group. In this case the T-statistic is likely be low, about 1 or less. On the other hand the group could be composed of people between 36 and 42, who as a group, just happen to have an average age of 40, but in this case 40 is fairly representative of anyone in the group. In this case the T-statistic is likely to be high, about 2 or more. The higher the T-statistic, the more likely it is that a group's summary number or average is a good representation of the parts that make up the group. Statisticians express the same idea by saying "the beta is statistically different from zero."

28, 29 30

#### Q. What is the economic significance of the betas' values you found?

31 32 33

34 35

36

37

38

39

A. All the values are far less than 1, which means that AGL and the comparable companies are far less risky investments than the market as a whole. In addition, the values do not vary much for any particular company, which means that investors do not perceive any substantial change in risk for these companies.

#### O. How did you derive the betas?

A. I used the monthly percentage change in the S&P 500 index to represent the market-wide return and the monthly percentage change in the company's stock price to represent the company's return. The change is calculated as: Price at the end of the month divided by price at the beginning of the month -- the result is converted to a natural logarithm and then the beta is calculated.

Q. Did you compare your betas to those estimated by anyone else?

21.

A. Yes. My betas are larger than those estimated by Dr. Andrews for his companies, shown at Schedule 9 of his direct testimony. The average for his betas is .27. This figure includes 5 negative betas. When Dr. Andrews implements his model he excludes the negative betas and raises his average to .41, which is still lower than the average of my betas, .458.

Q. Is the value of .458 a reasonable value?

A. Yes.

THE APPROPRIATE RETURN OF 10.55% COMPENSATES FOR MONTHLY COMPOUNDING

33 Q. What is the range of annual equity returns that 34 you have established?

36 A. I have established a range of 10.4% to 11.14%.

Q. In your opinion, within the range of 10.4% to

#### 11.14% what value is appropriate?

2

**4** 5

6

7

1

A. In my opinion the appropriate annual value is 10.55% because this compensates for monthly compounding that creates annual returns. Even though the range's mid point is about 10.8%, this can be converted into a return of 11.3%, an amount well-beyond my upper limit of 11.14%.

8 9 10

Q. Are there other experts who believe that annual returns are achieved by compounding monthly returns?

12 13 14

15

16

17

18

19 20

21 22

23

24

2526

27

28

11

Yes. This financial principle pervades the data Α. in SBBI-97, Ibbotson's 1997 Yearbook. For example, my Schedule 12, column (3) for the year 1996 shows a value of .2307 or 23.07%. My Schedule 17 shows exactly how .2307 is derived. This process is exactly the same as the one shown in my Schedule 6. Monthly compounding is the basis for all the annual returns shown in Dr. Andrew's Schedule 10 and my Schedule 11. But this is normal because SBBI-97 at page 49 explicitly says: "Annual total returns...for each asset class are formed by compounding the monthly returns." Thus in my Schedule 12. column (2) for the year 1996, the amount of 1370.95 equals 1.2307\*1113.92, or stated in words:

29 30 31

32

33

Annual Return This Year Equals: 12 Most Recent Monthly Returns Multiplied Together, Which Are Then Multiplied by Annual Return Last Year.

34 35 36

37

38

39

Returning to Schedule 17, it is important to notice that .2307 is larger than the sum of the monthly returns in column (2). If those returns were added together they would sum to only

.2148. This is further proof that annual returns are actually achieved by multiplying monthly returns together, i.e., monthly compounding. This also substantiates the findings in my Schedule 6, where an allowed annual return of 10.55% is subdivided into monthly returns that actually yield 11.0% over a 12 month period.

### Q. Isn't it true that monthly compounding introduces an upward bias to a prospective annual rate of return?

Yes, and here is how the bias occurs. Lets say Α. that TRA surveillance form 3.03 line 27 for a month shows an annual return of 11% for a If there is agreement that certain company. annual returns are formed by monthly compounding, then we know that the sum of the monthly returns is 10.55%, but when the returns are multiplied together the annual return is 11%. Now suppose that the company files a rate case and asks for an 11.5% return. If the proposed rate of return were subdivided on a monthly basis, the sum of the proposed monthly returns should be 11% to ensure that when they are compounded monthly, the result does not exceed 11.5%. If the monthly returns sum to 11.5%, then in effect, the allowed rate of return is 12%.

Another way to understand the compounding effect is to consider how the test year rate base is calculated. The rate base is actually an average of the rate base at the beginning of the test year and the rate base at the end of the test year. Thus the value of rate base already includes 6 months of reinvested earnings. Therefore, when a rate of return is

applied to the rate base, the company is actually earning on its earnings. This is another way to achieve monthly compounding. If this aspect were implemented in terms of Schedule 6, the beginning balance would not be \$1 but about \$1.06.

Q. Is there any document in this docket where a proposed annual return is subdivided on a monthly basis?

A. The only one I know of is my Schedule 6.

Q. What equity return do you recommend in this case?

A. I recommend a rate of 10.55%, an amount between my DCF rate of 10.4% and 11.14%, the risk premium rate. I choose 10.55% because I know that monthly compounding gives the company the opportunity to earn a higher return. I also choose 10.55% because I know that the rate base already includes 6 months of reinvested earnings before the rate of return is applied to the rate base, thus giving the company another opportunity to earn a higher return

Q. What compounded return can the company earn with an annual rate of 10.55%?

A. The monthly compounding process gives the company an opportunity to earn approximately 11.0%.

CAPITAL STRUCTURE AND OVERALL RATE OF RETURN

Q. What are your findings regarding capital structure?

The capital structure in this case appears in A. the company's filing as Exhibit 5, Schedule 9. Since the amounts in that schedule are derived from AGL's capital structure, CA data request 42 asked the company to provide support for the calculations. The company's response is attached to my testimony as Schedule 18. of the projected balances in that document are explained or supported by the company. For example, the preferred stock balance in 1997 is \$58.4 but the projected balance in 1998 is \$70 million. Despite this hefty increase, no explanation is provided. Continuing with this example, AGL's long term debt is shown as \$659.5 million in 1997 and 1998. However, the company's response to CA data request 24 showed a balance of \$584.5 million as of April 1997. This is an unexplained difference of \$75 million. In addition, the new debt's interest rate is not provided. Also, according to the company's response to CA data request 23, all long term debt and preferred stock is held by AGL instead of its parent holding company, AGL Resources. Therefore, the \$75 million cannot be attributed to debt issues by the holding company. Finally, AGL's response to data request 42 does not show how the amount of the CG capital structure, \$95.8 million, is derived. Instead, the response shows how \$95.8 is allocated to the different aspects of the capital structure.

33 34

35 36

37 38

39

In sum, the amounts shown in Schedule 18 are different than what I expected, but I do not believe the differences are material to my analysis, which relies on the portions and the estimated costs. However, my recommended overall return is neither an endorsement nor an

acceptance of the rate base that will be
applied to the overall return. To the extent
that the projections in Schedule 18 are not
supported, the company's filed rate base is
questionable.

Q. What weighted overall capital cost do you recommend?

10 A. In my opinion a cost of 8.85% before compounding, shown in Schedule 19.

Q. What compounded overall return can the company earn with an annual rate of 8.85%.

A. The company has an opportunity to earn about 9.3%.

#### ANALYSIS OF METHODS EMPLOYED BY THE COMPANY'S COST OF CAPITAL WITNESS

Q. You have stated that you disagree with Dr. Andrews' analysis, can you explain your reasons?

A. Yes. At page 4 lines 22-23 of his direct testimony he states: "I measure the costs of equity capital of ...small publicly held gas distributing companies and impute their cost of equity to CGC." I have already pointed out an obvious difference between these companies and CG -- they are independent financial entities who have actively traded stock while CG has no actively traded stock because it is a wholly owned subsidiary of AGL. This alone suggests that his analysis is inappropriate. However, after scrutinizing his testimony and his data

sources, I conclude that his equity returns -- 14.39%, 14.38%, 14.23%, 12.5%, 12.17% and 11.06% shown at page 47 of his testimony -- are based on an irrational analysis.

#### SMALL COMPANY APPROACH IS IRRATIONAL

#### Q. Why is the analysis irrational?

A. The small company data base that he uses does not represent the performance of small companies. Instead, the data base represents the performance of one particular mutual fund out of more than 200 funds that specialize in buying and selling small company stocks. The particular mutual fund used by SBBI-97, the very same one that Dr. Andrews uses, is named the Dimensional Fund Advisors 9-10 Small Company Mutual Fund (DFA 9-10 fund). SBBI-97 at page 51 says; "...the small company stock returns series is the total return achieved by the Dimensional Fund Advisors (DFA) Small Company 9-10 Fund."

However, the fund requires an initial purchase of \$2 million dollars. This is well beyond the means of stockholders who own the companies used by Dr. Andrews. The fund also has a highly unusual ownership concentration, one that is certainly not representative of a gas distribution utility. In 1996 the fund had assets of \$1.18 billion with over \$625 million held by five owners that are actually pension funds:

38 OWNER

OWNERSHIP PERCENTAGE

Charles Schwab & Company Inc.	31.44%
State Farm Insurance	10.76%
Pepsico Inc. Master Trust	8.87%
Owens-Illinois	5.48%
National Electrical Benefit Fund	5.26%

This ownership pattern and the \$2 million minimum investment clearly indicates that the so-called "returns to small companies" are actually returns to well-financed pension groups rather than being a return that is accessible to ordinary investors. There would be no incentive for anyone to make a \$2 million minimum investment and buy into the DFA 9-10 fund if such returns were accessible to ordinary investors. Also, these returns are derived from the capital gains made by the constant buying and selling of stock, a far different process than the way in which a gas distribution company makes money.

However, even the returns themselves are open to question because the methods used to calculate the fund's return are not equivalent to the return-on-assets concept used in utility regulation. In 1996 the fund's return on assets was 8.75%. Dr. Andrews' Schedule 6, page 1, the far-left column titled "Small Company Stocks" shows the return as 17.62%. He uses this amount and the remaining figures in that column to develop the return differentials of 9.16%, 7.57% and 6.86% shown on the right side of the schedule. Those amounts are repeated in Schedule 6 page 2 and in his direct testimony, at the bottom of page 45 under the column titled "Equity Diff" and lead to a huge cost of equity, 14.3%.

These figures are not credible, not only for the

reasons I have just discussed, but also for the overlapping directorates of the DFA 9-10 fund and SBBI-97. Mr. Robert G. Ibbotson is the Chairman and President of Ibbotson Associates, and the publisher and author of SBBI-97. He is also on the Board of Directors of the DFA 9-10 fund. This strongly implies that the small company data used in SBBI-97 is not derived from an independent source and that the data may overstate the actual returns. This possibility is already substantiated by the difference between 8.75%, the return on assets, and the so called return of 17.62% used by Dr. Andrews. Mr. Ibbotson's dual role is indicated in the Statement of Additional Information published March 28, 1997, as a supplement to a prospectus issued the same date by DFA Investment Dimensions Group, Inc. 

These factors demonstrate the extraordinary weakness in the small company analogy that Dr. Andrews uses to estimate the cost of equity. But there is another contradiction in the data: in 1994 only 9 of Dr. Andrew's companies were owned by the fund, in 1995 and 1996 only 11 of the companies were owned by the fund. Thus half of Dr. Andrews' companies are not considered "small" by the fund itself.

Taken as whole these factors make it plain that the small company analogy is an irrational approach to setting the equity return in this docket. In my opinion the TRA should disregard the results of Dr. Andrews' small company analysis, shown in his direct testimony at the bottom of page 45.

Q. What are sources of data that support the assertions you have made?

- 1 A. My data is taken from four different sources:
  - 1. DFA Investment Dimensions Group Annual Reports for the Years Ended November 30, 1996 and November 30, 1994 and DFA's SEC10K filing for 1995.
  - 2. Statement of Additional Information, Supplement to DFA's Investment Dimensions Group, Inc. Prospectus of March 28, 1997.
  - 3. Morningstar, Inc.'s Reports on Mutual Funds, as of May 31, 1997.
  - 4. SEC Form 10Ks and 10Ka-1 for Dr. Andrews' companies and the DFA Group.
  - Q. What is Morningstar Inc.?

- A. Morningstar is a software and data base firm that
  maintains records on over 8000 mutual funds and
  tracks their performance. The company is located in
  Chicago.
  - Q. What schedules have you set up from this data?
  - A. Schedule 20 is a summary of Morningstar's reports on 230 mutual funds that specialize in buying and selling small company stocks. About 30 concentrate on foreign stocks and the remainder focus on domestic stocks. The funds are arranged in descending order according to the amount of the initial minimum investment. The funds managed by the DFA group are among the most expensive funds to purchase. Nearly all of DFA's funds require \$2 million minimum investment. For all 230 funds taken as a group, there is a systematic difference between the

rate of return on assets and the 1996 return as reported by the funds. The return on assets is much lower than the other so-called return.

1

2

3

**4** 5

6

7

8

9

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

30 31

32

33

34

35

36

37

38

39

This discrepancy was so large that I was compelled to cross-check the accuracy of the Morningstar report on the DFA 9-10 fund against the data in the DFA 1996 annual report. The Morningstar report is Schedule 21 and the DFA report on the fund is Schedule 22. Although the data is not identical they are close enough to be substantially the same. For example, Morningstar reports assets of \$1107 billion and the DFA annual report shows assets of \$1181 billion. In Schedule 21 I have highlighted the portfolio statistics showing an exact match between Morningstar's data and DFA's. This suggests that Morningstar's calculation of a return on assets is credible even though the DFA report does not provide this measure. Also, the DFA report, the line titled "Net Gain (Losses) on Securities (Realized and Unrealized)" represents capital gains and losses by the fund. Clearly, the fund is completely dependent on capital gains to make a return, unlike a gas distribution company that sells a product and a service. This, too, makes the fund an unreasonable basis to develop returns for a gas distribution company.

Schedule 23 shows DFA's <u>Statement of Additional Information</u>, the cover page and pages 20-22. The fund's method of calculating a return is shown from Schedule 23 page 3, at the bottom, to the schedule's page 4 at the top. The description is vague and not articulated through any readily understood example. This sharply contrasts with the way all parties calculate the return on assets that a gas

distribution utility receives. Therefore,
returns to mutual funds, such as the amounts in
Dr. Andrews' Schedule 6, page 1, the far-left
column titled "Small Company Stocks," cannot be
used to estimate the <u>return-on-assets</u> that is
granted to a gas distribution company.

 Schedule 24 shows DFA's <u>Statement of Additional Information</u>, pages 10, 11 and 15, which respectively list the company directors and the major owners of the fund. Mr. Ibbotson's name appears at the second page, the third listing from the top. This confirms that the DFA 9-10 fund and SBBI-97 have overlapping directorates. Page 15 confirms the ownership pattern of the fund.

 Q. How do you know that investors in Dr. Andrews' 22 small companies would be unable to buy into the DFA fund?

A. My opinion is based on the data I gathered about Dr. Andrews' companies. Schedule 25 column (6) shows the average value of the holdings per shareholder for Dr. Andrews' companies. The maximum value is \$53,171 and the average value is \$28,195. The DFA fund's initial investment is \$2 million, about 50 to 100 times larger than the values shown in column (6). It is impossible for stockholders of Dr. Andrews' companies to buy into the DFA fund.

Q. How do you know that the DFA fund included only half of Dr. Andrews' small companies?

A. I acquired DFA's annual reports for 1994 and 1996 and the company's SEC 10K filing for 1995. Those reports list the companies in the fund.

Schedule 26 shows the results.

3 4

Q. Is it your opinion that Dr. Andrews actually used the 22 "small publicly held companies" to estimate the equity returns of 14.3%?

5 6 7

8

9

10 11

12 13

14 15

16

17

18

19

20

21

No, Dr. Andrews did not use those companies. Α. In my opinion he used the concept of "small companies" to make a link with the purported returns of the DFA fund, which is the real source of the huge equity-return estimates that appear in his direct testimony at the bottom of page 45. Also, nine of Dr. Andrews' companies do not fit the definition of a small company that is given by SBBI-97 at page 136: A small company is one with a market value less than \$197.4 million as of September 1996. My Schedule 25 shows 9 of Dr. Andrews' companies exceeding that value on April 30, 1997. This strongly suggests that Dr. Andrews' companies are composed of two dissimilar groups that are viewed differently by the market.

22 23 24

### RETURNS OF 12.5% AND 12.17% ARE BASED ON LARGE COMPANY DATA, MISUSE OF DATA AND IRREGULAR, UNSUPPORTED PROCEDURES

262728

25

Q. Are Dr. Andrews' other returns derived from the small company concept and the DFA fund?

29 30 31

32

33

34

35

36 37

38

A. No. He uses large companies to derive the returns of 12.5% and 12.17%. The returns appear in his testimony at page 44 lines 21-22 and at page 45 lines 1-2 and are derived from his Schedule 10. The schedule's left side has a column titled "Common Stock Total Returns." This name is wrong. In his note at the bottom of the schedule he says data for the years

1987-1995 is drawn from "Exhibit A-1" of Ibbotson's 1996 yearbook. The correct name is "Table A-1 Large Company Stocks: Total Returns." A portion of the table from the 1996 yearbook is attached to my testimony as Schedule 27. Note the title of column (3) in my Schedule 11 and the exact match between the amounts in column (3) from 1988-1996 and the amounts listed in Dr. Andrews' so-called "Common Stock Total Returns."

Contrary to his assertion, "I measure the costs of equity capital of ... small publicly held gas distributing companies," Dr. Andrews uses large companies without acknowledging the fact nor explaining why he has done so. This undermines his entire analysis, making it an irrational basis to determine a return to equity.

#### Q. Does Dr. Andrews use the data correctly?

 A. No. He limits Schedule 10 to a history of 10 years instead of a 71 year history recommended by SBBI-97.

#### Q. Are you suggesting that every recommendation of SBBI-97 has to be followed?

A. No. Although SBBI-97 is a useful tool and an authoritative source for some aspects of developing a rate of return, its authors are fallible, as I have already demonstrated with regard to the small company issue. However, it is contradictory to invoke an authoritative source to justify one position and then depart from the source's recommendations in other positions without explaining the reasons for the departure.

Dr. Andrews has departed from the standard practice of using a 71 year history to derive the risk premium differential. His direct testimony offers neither a justification nor an explanation of his reasoning. In their absence, his choice of a 10 year history appears arbitrary and calculated to increase the estimated cost of equity.

 For example, his Schedule 10, the line titled "Averages" shows that: .1604 - .0778 = .0826. These values appear in his direct testimony at page 44 line 21:

$$K_e = .0133 + .0778 + (.41)*(.1604-.0778)$$

$$K_e = .125 = 12.5$$
%

 However, if Dr. Andrews had taken the data for the 71 year period, as the source recommends, the averages would be different than what he shows in Schedule 10.

The figure of 16.04% would decrease to 12.7%, which is the average return to large companies and which is shown in my Schedule 11 at the bottom of column 3. The figure of 7.78% would decline to 5.2%, which is shown in my Schedule 14 in the line titled "Income Portion of Long-Term Government Bonds" and under the column titled "Biased Average." If these new figures were applied to his equation at page 44 line 21, the new result would be:

$$K_e = .0133 + .052 + (.41)*(.127-.052)$$

$$K_e = .0961 = 9.61$$
%

A similar result occurs in the equation at line 1 of page 45 of his direct testimony, where the

new value would be 9.31%.

 The use of a 10 year history is vital to Dr. Andrews' results. However, the exact reason he chose this period is not discussed in his testimony. Therefore, I recommend that the TRA disregard the estimates of 12.5% and 12.17% because they are arbitrary and unreasonable.

In fact, his formulation of the risk premium model is irrational.

#### Q. Why is his risk premium model irrational?

A. Dr. Andrews' model is irrational because it is not tied to the debt markets faced by AGL, the "A" rated bond market, despite his lengthy discussion of AGL's debt quality at page 18 of his testimony. The only place in his analysis where he uses "A" rated corporate debt is in a DCF analysis appearing in his testimony at page 46 lines 16-17, which shows returns of 8.98% and 9.35%. These figures are repeated at page 47 lines 7-8, where he describes these numbers as "DCF Over Various Debt Instruments."

This portion of his testimony contradicts a statement in his deposition of September 9. In that deposition, from page 43 line 24 to page 44 line 3, he states: "One of the lines of analysis that I pursue is the equity over debt cost approach, risk premium approach; and I used some of the costs of the debt that Atlanta Gas had outstanding and found differentials of equity cost over that." However, Dr. Andrews has not used AGL's debt or "A" rated bonds in any risk premium analysis, but only in the DCF analysis he describes at pages 46 and 47 line 7 of his testimony. His highest set of returns —

14.23%, 14.38% and 14.39% derived from his small company analogy, and his second highest set of returns -- 12.5% and 12.17% -- are completely unrelated to the "A" bond market or to AGL's debt.

#### Q. Is your risk premium model rational?

A. Yes. My risk premium model is based on the general principle that equity returns have to be compared to and exceed corporate debt. In this particular case the debt in question is the "A" bond market. If I expressed the principle instead of the numbers, the model would be:

 $K_e$  = Current Cost of A Rated Utility Bonds  $(R_m-R_f)*(B_e)$ 

Dr. Andrews' model does not begin with corporate debt. Instead, his model begins with the concept of "Long-Term U.S. Govt. Bonds Income Component Returns." If I expressed his idea instead of the numbers, his model would look like:

 $K_e = 1.33\%$ +Long-Term U.S. Govt. Bonds Income Component Returns +  $(R_m - R_f) * (B_e)$ 

Therefore, Dr. Andrews' model is based on the idea that equity returns have to be compared to and exceed the returns of long term government bonds instead of corporate debt. This is an irrational basis to begin an analysis because returns to government bonds are always lower than returns to corporate bonds. My Schedule 14 clearly shows that corporate bonds outperform government bonds. Therefore, Dr. Andrews' model

has a starting point that is bound to be lower than the starting point in my model. However, he raises the starting point of his model by resorting to a figure of 1.33%. This amount is not related to debt, corporate or government; nor is it related to equity returns of either large or small companies.

#### Q. What does the 1.33% relate to?

A. The figure is not related to anything because it is a nonsense-number.

#### Q. How is 1.33% a nonsense-number?

A. Dr. Andrews explains the derivation of 1.33% in his direct testimony, page 44 lines 13-14. The derivation is irrational for two reasons:

1. Dr. Andrews is dealing with numbers that cannot be treated as if they are "per day, per week, per month or per year" numbers. Just as the assertion - "You are 6 feet tall per month, so in 12 months you will be 6X12=72 feet tall per year" -- is nonsense, so too is Dr. Andrews' number of 1.33%.

This point becomes clear by examining his derivation of 1.33%. In his Schedule 9 under the "Alpha" column, there is a number, .0011, which is the average of the alphas that have a positive beta. Thus .0011 is the basis for deriving .0133 by the formula at page 44 lines 12-13 of Dr. Andrews' direct testimony:

 $.0133 = (1 + .0011)^{12} - 1$ 

Although he does not say that he is deriving his alphas from five years of monthly data, he is. At page 42 lines 6-12 of his testimony Dr. Andrews explains that he derives his betas with five years of monthly data, but every time a statistical regression produces a beta an alpha is created too. This is why his work and mine both have alphas as well as betas.

He treats the value .0011 as if it were a monthly value that can be compounded into an annual figure. This is why he uses 12 in his formula:

$$.0133 = (1 + .0011)^{12} - 1$$

The alphas and betas are derived from the same data and the same months. If the alpha is a monthly rate, isn't the beta a monthly rate, too? If the beta is not a monthly rate, how can the alpha be a monthly rate? If his beta of .41 were compounded monthly the result would be:

$$60.75 = (1 + .41)^{12} - 1$$

If this value were placed into Dr. Andrews' original formula the cost of equity would be:

$$K_e = .0133 + .0778 + (60.75)*(.1604-.0778)$$

$$K_e = 5.10 = 510$$
%

60.75 is produced in exactly the same way as Dr. Andrews' produced .0133. If

60.75 is dismissed as incredible or fictitious, then its counterpart, the "annualized" alpha, is an unreasonable number and .0133 should be rejected, too. Both numbers are unreasonable. It is irrational for Dr. Andrews to treat the alpha as a monthly figure that can be compounded to an annual one. His treatment further suggests that the alpha can be compounded according to the time frame of the data used, i.e., if the alpha and beta are derived from monthly data then the alpha can be compounded monthly, but if the data is weekly, then the alpha can be compounded weekly. This too is irrational.

For example, if I took the weight of 22 people each month for 60 months and then took an average, I can say "based on monthly data the average weight per person is 150 pounds" but it would be wrong to say "because I collected my data on a monthly basis each person weighs 150 pounds per month and 1800 pounds per year." This is the exact logic that Dr. Andrews employs. The difference between this example and Dr. Andrews' irrational procedure is the size of the numbers.

If the beta is .41, as in Dr. Andrews' results, then the value of the company's stock changes 41 cents per \$1 change in the market's value, whether the market's change is measured over a day, a week, a month or a year -- .41 is not compounded to

a higher figure nor reduced to a lower one. The same logic applies to the alpha.

In my opinion the TRA should disregard Dr. Andrews' figure of 1.33% because it is irrational.

2. Dr. Andrews' direct testimony does not provide any tests of statistical accuracy for the alphas in his Schedule 9. In the absence of this data, my opinion is that the alpha should be presumed to be zero.

Earlier I said that every time a statistical regression produces a beta a so-called "alpha" is created too. Since his overall positive beta is .41 while mine is .458, I expected this similarity to be carried through to the alphas, and it is. The values of his alphas are very close to zero, just as they are in my analysis, at Schedule 15 page 3. However, page 4 of Schedule 15 shows the alphas' statistical measures of accuracy, the T-statistics. They are tiny, meaning the alphas are no different than zero.

The typical pattern of alphas, betas and their statistical accuracy are provided in the table below.

Betas	Alphas
Positive Values	Very Close to Zero- May Be Positive or Negative

High T-Statistics Indicate
Accuracy

Low T-Statistics Indicate Inaccuracy

Schedule 15 fits this pattern. Dr. Andrews' data should show the same pattern, at least for his positive betas.

When the alphas are no different than zero, they do not add anything to the cost of equity, and there is no need to use the alphas. In this case the formula looks like:

$$0 = (1 + .0000)^{12} - 1$$

The alpha is zero. This is why alphas are thought of as having no value and no meaningful economic interpretation and why they never appear with betas.

I do not know of any financial publication that provides betas <u>and alphas</u> nor do I know of any model that treats the alphas the way Dr. Andrews does.

- Q. Did you ask Dr. Andrews to provide the tests of statistical significance for the alphas and betas that he calculated?
- A. Yes. He did not supply them, consequently his conclusions are not supported by material and substantial evidence. His response is attached to my testimony as Schedule 28.
- Q. Do you have any comment regarding his response?

 A. Yes. Since Dr. Andrews has not provided the tests of statistical significance, I am even more concerned that his alphas are really no different than zero. In my analysis the alphas are zero and they are not statistically significant. Also, it is contradictory for Dr. Andrews to calculate sums and averages for the betas and alphas, as he does in his Schedule 9, and then state in his response: "Tests of significance, such as T-statistics from the regressions related to individual stocks cannot be summed or averaged across the composite." I have done exactly that in my analysis. In fact, its results are appropriate.

#### Q. Why are your results appropriate?

All my betas are positive. They are estimated Α. over twelve contiguous 60 month periods, with the first period ending in May 1996 and the last one ending in April 1997. This procedure captures any change in how the company's beta value is responding to the market. I provide tests of statistical significance, and the tests are reasonable. The alphas are zero, their tests of statistical significance indicate the true values are zero, and they play no role at all in my return. All of these factors taken together reinforce the implications of my Schedule 1, which demonstrates the comparability of my group of companies.

In comparison, Dr. Andrews' analysis has 5 negative betas, which he dismisses as "analytically indefensible" at page 43 line 18 of his direct testimony. Dr. Andrews does not explain why the results are "indefensible," but

it is clear that if he did not exclude the negative values, his estimated return of 12.5% would be lower. Therefore, the negative betas appear to be indefensible because they would lower the company's return. He relies on the alpha to raise his estimated returns and performs an irrational procedure to boost an estimated return by 1.33%. In addition, he does not provide tests of statistical significance, even when asked to do so. Taken together, these factors indicate that Dr. Andrews' companies do not form a comparable group that is a rational basis for estimating a rate of return. These factors further reinforce what my Schedules 25 and 26 already suggest --his companies are composed of two dissimilar groups that cannot be a rational basis to set a rate of return in this docket.

Q. What is your opinion regarding Dr. Andrews' statistical analysis is shown in Schedule 9 of his testimony?

A. In my opinion the TRA should disregard the conclusory analysis because it is arbitrary, irrational and unsupported by material and substantial evidence. Therefore, his analysis cannot constitute a basis for a decision.

#### DCF ANALYSIS IS BIASED UPWARDS

Q. What is your opinion of Dr. Andrews' DCF analysis?

A. His DCF recommendation of 11.06% is derived from Schedule 8, page 2, of his testimony. My opinion is that his result is biased upward by approximately 2% because his rate of 11.06% is

1 based on only 4 companies instead 21. He 2 ignores the results of the 17 other companies 3 that he consider's as comparables. Therefore, 4 his recommendation of 11.06% is not 5 representative of the group that he has 6 designated as comparables. On the other hand, 7 if his companies are composed of two groups not 8 comparable to each other, then his decision to 9 ignore some would be rational. However, if this 10 is why he has ignored 17 companies, then this 11 makes all his other analyses irrational, too. 12 For example, of the 17 companies ignored in Schedule 8, 12 of them are used in his Schedule 13 9 to derive the returns of 12.5% and 12.17%. On 14 15 its face this is clearly an irrational 16 procedure, and Dr. Andrews offers no 17 explanation. It is my opinion that the TRA should disregard his recommended DCF rate 18 19 because it is biased and not supported by 20 material and substantial evidence. 21

22 23

#### RANGE OF 11.5% TO 12.5% IS IRRATIONAL

2425

26

Q. Do you have any concluding opinions regarding the equity returns suggested by the company's cost-of-capital witness?

27 28 29

30

31

32

33

34

35

A. Yes. In his direct testimony, at page 47 lines 14 and 23, Dr. Andrews concludes his analysis by recommending a range of 11.5% to 12.5%. Dr. Andrews suggests this is a reasonable range because he has found returns that are well above the range. At page 47 lines 18-22 Dr. Andrews says "The Small Stock equity risk premiums...over 14%...cannot be dismissed."

36 37 38

39

The "small company" premiums can and should be dismissed because:

They are based on 1 mutual fund out of 200;

The fund has a minimum investment requirement of \$2 million;

The stockholders of Dr. Andrews' companies cannot afford to buy into such a fund;

The directorates of the Ibbotson Associates and the DFA 9-10 fund overlap - suggesting that the funds' return is not calculated by an independent source;

The fund's return on assets is only 8.75%, an amount provided by Morningstar Inc., a source that is independent of Ibbotson Associates and DFA Investment Dimensions Group - the manger of the DFA 9-10 fund;

The difference between the fund's return on assets and its so-called annual return means that a mutual fund's return cannot and should not be used to grant a utility's return on assets;

The fund relies exclusively on capital gains as the source of its return.

The small-company fund approach is an unfit and irrational method to develop a rate of return that must be supported by ratepayers.

The returns of 12.5% and 12.17%, both are predicated on data that is specific to large

companies - not small ones. This invalidates both returns because Dr. Andrews' analysis is based on "small publicly held" companies. Also, I have pointed to several places in the derivation of 12.5% and 12.17%, where Dr. Andrews is silent about the logic that led him to perform crucial procedures or where the procedure is irrational. Considering all these factors, Dr. Andrews' recommended range of 11.5% to 12.5% emerges as irrational. 

Q. What is your opinion regarding Dr. Andrews' returns of 14.39%, 14.38%, 14.23%, 12.5%, 12.17% and 11.06%?

A. In my opinion, the returns of 14.39%, 14.38%, 14.23%, 12.5%, 12.17% and 11.06% are unsubstantiated, speculative and more than just and reasonable. They cannot be a basis for the TRA to set the equity return in this docket.

Q. How is your testimony different from that of the company's cost-of-capital witness?

A. In my opinion my testimony is different because I have used reasonable methods and achieved reasonable results. I have explained my methods in pain-staking detail, giving all parties an accurate and true description of all the factors and sources I considered when forming my opinion on the rate of return. Therefore, the equity return of 10.55% is neither confiscation nor extortion an is equitable to ratepayers and the company alike.

Q. Does this conclude your direct testimony?

38 A. Yes.

# **Proof of Comparability**

## Market Statistics

Average Number Of Years Market Stock Is Value Held By 4/30/97 Investor \$(Millions) 3 6 1061 3 86 343 2 26 1352 4 25 548 3 98 388 2 98 545 2 21 1167 3 37 687	Value of Holdings Per Share Holder 4/30/97 \$63,334 \$30,949 \$42,951 \$58,122 \$35,410 \$44,355 \$34,172 \$37,664	Dividend Yield Dec 1996 5 40% 5 61% 5 45% 5 45% 5 45%	Equity Ratio Dec 1996 48 9% 53 1% 55 8% 57 1% 57 1% 56 4%	Markel Price to Book Price to 1996 180% 150% 149% 149% 161% 171%	NAME  AGL RESOURCES INC BAY ST GAS CO BROOKLYN UN GAS CO INDIANA ENERGY INC LACLEDE GAS CO NORTHWEST NAT GAS CO PEOPLES ENERGY CORP PIEDMONT NAT GAS INC
---	--	---	--	--	--

# Financial Behavior

PEOPLES ENERGY CORP PIEDMONT NAT GAS INC WASHINGTON GAS LT CO AVERAGE	BAY ST GAS CO BROOKLYN UN GAS CO INDIANA ENERGY INC LACLEDE GAS CO NORTHWEST NAT GAS CO	80% - Sources INC	Value Line March 31, 1995 "We advise staying with top quality stocks with payout ratios below 80% VVe'd be
83 4% 97 8% 92 1% 97 9%	99 2% 87 6% 82 9% 93 8% 167 3%	1991 98 1%	<b>▼</b>
85 4% 65 0% 84 3% 97 9%	96 5% 95 6% 82 8% 102 6% 155 0%	1992 91 2%	ompanie oncerns
84 4% 65 5% 83 2% 80 7%	80 0% 76 3% 77 3% 75 8% 67 0%	1993 96 3%	es Resp of The
84 5% 74 8% 78 2% 80 1%	77 8% 73 0% 66 7% 85 9% 72 1%	1994	ond In S
101 1% 73 8% 77 2% 83 3%	86 5% 73 2% 73 3% 97 6% 73 1%	991 1992 1993 1994 1995 1996 91% 91 2% 96 3% 88 9% 78 2% 77 4%	Companies Respond In Similar Way To Concerns Of The Financial Community
61 8% 68 9% 61 6% 66 7%	76 0% 72 4% 59 4% 67 4% 60 9%	1996 77 4%	ay To runity

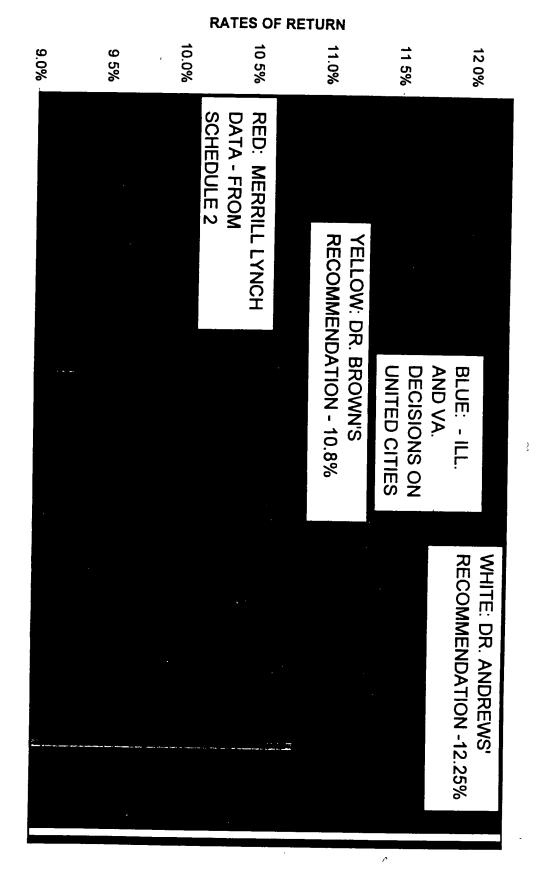
{

Docket No 97-00982
Exhibit CA SNB
Direct Testimony
Schedule 1
Page 1 of 1

## Docket No 97-00982 Exhibit CA-SNB\_\_\_\_ Direct Testimony\_\_\_

Chart 1 of 3

## ESTIMATIONS OF REQUIRED RATES OF RETURN TO EQUITY FOR AGL'S SUBSIDAIRY - CHATTANOOGA GAS



## **Merrill Lynch Data**

Mar-97 Apr-97 May-97	Dec-96 Jan-97 Feb-97	Sep-96 . Oct-96	May-96 Jun-96 Jul-96 Aug-96	Jan-96 Feb-96 Mar-96 Apr-96	Feb-95 Mar-95 May-95 Jun-95 Jul-95 Aug-95 Oct-95 Nov-95	MONTH
10 5% 10 5% 10 5%	10 4% 10 2% 10 2%	96% 96% 95%	9 9% 10 0% 9 7%	9 9 8 8 6 9 1 8 8 8 8 % % % %	10 6% 10 3% 10 1% 10 1% 10 3% 10 3% 9 4%	DCF RATE
10 1% 10 3% 10 1%	9 4% 10 6% 10 0%	9 9% 9 7% 9 5%	9 7% 9 8% 9 7%	9 3 % 9 3 % 9 7 %	9 4% 9 6%	RISK PREMIUM RATE
10 5% 10 5% 10 5%	10 4% 10 6% 10 2%	99% 97% 95%	9 9% 10 0% 9 7%	9 9 3 % 9 3 % 9 3 %	10 6% 10 3% 10 2% 10 1% 10 3% 10 3% 9 6%	MAXIMUM OF THE TWO RATES

Source Memil Lynch Quantitative Profiles [Published Monthly]

January 1995 through May 1997 Issues, page 11

Docket No 97-00982
Exhibit CA-SNB\_\_\_\_
Direct Testimony\_\_\_
Schedule 2 \_\_\_\_
Page 1 of 1 \_\_\_\_



i	nĺ	Os	,44	k.
•				





Docket No. 97-00982
Exhibit CA-SNB\_\_\_\_
Direct Testimony\_\_\_
Schedule 3\_\_\_
Page 1 of 1

## i wish communication

Click here

## United Cities granted rate increase in Illinois 03 24 pm Jun 26, 1967 Eastern

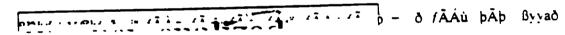
BRENTWOOD, Tenn.--(BUSINESS WIRE)--June 26, 1997--United Cities Gas Co. (NASDAQ.UCIT), a multistate distributor of natural and propane gas, announced today that the Illinois Commerce Commission has granted the company a rate increase of \$428,000 in annual revenues.

An overall rate increase of 2.09 percent was granted for approximately 23,000 customers in or near Harrisburg, Metropolis. Vandalia, Virden and Salem, Ill. The rate increase provides United Cities with a 9.85 percent return on rate base and a 10.94 percent return on common equity. The increase is the result of an application filed before the Commission in November 1996.

The net rate increase is part of an agreement reached by United Cities. Atmos Energy Corporation and the Commission in approving the merger of United Cities and Atmos. In addition, the rate increase will be followed by a three year rate moratorium.

United Cities Gas Company distributes natural and propane gas to approximately 350,000 customers in 10 states. The company is also engaged in other energy-related businesses (See also <a href="http://www.businesswire.com">http://www.businesswire.com</a>)

Copyright 1997 Business Wire



Docket No. 97-009	R2
Exhibit CA-SNR	
Direct Testimony_	_
Schedule 4	-
Page 1 of 1	

United Cities granted rate increase in Virginia 35 03 pm Jun 02 \*997 Eastern

BRENTWOOD Tenn --(BUSINESS WIRE)—June 2 1997—United Cities Gas Co NASDAQ UCIT) a multistate distributor of natural and propane gas announced today that the Virginia State Corporation Commission has granted the company a rate increase of \$102 838 in annual revenues by order dated May 27 1997

An overalificate increase of less than one percent was granted for approximately 18 000 current regulated customers. The rate increase provides United Cities with a 10 percent return on rate base and an 11 percent return on common equity. The increase is the result of an application filed

Due to the Commission's decision, money over-collected from customers since Sept. 28, 1995, when Untied Cities began charging interim rates based on its original 3 percent rate increase request, will be credited to customers' accounts with interest. The credit amount for customers will vary according to their gas usage during the period interim rates were in effect.

United Cities' last rate increase in Virginia was granted in 1989. Since that time irate reductions were implemented in both 1991 and 1994.

United Cities Gas Company distributes natural and propane gas to approximately 350,000 customers in 10 states. The company is also engaged in other energy-related businesses. (See also, http://www.businesswire.com)

Copynght 1997 Business Wire

Docket No. 97-00982 Exhibit CA-SNB Direct Testimony Schedule 5 Page 1 of 1

This Schedule Left Intentionally Blank

## **LITECT OF MONTHLY Compounding**

	Aug-96	Jul-96	Jun-96	May-96	Apr-96	Mar-96	Feb-96	Jan-96	Dec-95	Nov-95	Oct-95	(1)		
)	-0,253	2,226	-1,122	0,836	5,232	13,797	14,495	18,120	17,476	9,492	3,272	(2)		Monthly Net Income for Atlanta Gas-FY 1996 *
	-0.3%	2 8%	-1.4%	1 0%	6 5%	17.1%	18.0%	22.5%	21 7%	11 8%	4 1%	(3)	-	Monthly Income as a Percentage of Annual Income
	-0.03%	0.29%	-0.15%	0 11%	0 68%	1 80%	1.90%	2 37%	2 29%	1 24%	0 43%	(4)	[col (3) X Allowed Annual Return of 10.55%]	Pattern of Monthly Return Based on Monthly Pattern of Income
	\$1.115	\$1.112	\$1.113	\$1 112	\$1 104	\$1.085	<b>\$1</b> 065	\$1.040	\$1.017	\$1.004	\$1.000	(5)		Cumulative Equity Balance at Start of Month
	-\$0 0004	\$0 0032	-\$0 0016	\$0.0012	\$0.0076	\$0 0196	\$0 0202	\$0.0247	\$0.0232	\$0 0125	\$0 0043	(6)	[col (4) X col (5)]	Monthly Return on Equity
	\$1 114	\$1 115	\$1 112	\$1 113	\$1 112	\$1 104	\$1 085	\$1 065	\$1 040	\$1 017	<b>\$</b> 1 004	(7)		Cumulative Month End Equity Balance

\*From CA Data Request 39

Sep-96 Aug-96

80,653 -2,918

100 0%

10.55%

-3 6%

-0.38%

\$1 114

-\$0.0043 \$0 1102

Direct Testimony Schedule 6\_ Page 1 of 1\_\_

	Direct Testimony Schedule 7 Page 1 of 2
1	BEFORE THE TENNESSEE PUBLIC SERVICE COMMISSION
2	
3	IN THE MATTER OF: Docket No. 9502116
4	CHATTANOOGA GAS COMPANY
5	
6	Tuesday, September 26, 1995 Hamilton County Board of Education
7	Chattanooga, Tennessee 37402
8	CROSS EXAMINATION OF DR. VICTOR L. ANDREWS
9	APPEARANCES:
10	COMMISSION MEMBERS:
11	Keith Bissell, Chairman, Steve Hewlett and Sara Kyle
12	
	FOR THE CHATTANOOGA GAS COMPANY:
13	William L. Taylor, Jr., Esq., of
14	Spears, Moore, Rebman & Williams
15	Eight Floor Blue Cross Building Chattanooga, Tennessee 37401
16	L. Craig Dowdy, Esq., of
	Long, Aldridge & Norman
17	One Peachtree Center, Suite 5300
18	303 Peachtree Street Atlanta, Georgia 30308
19	FOR THE CONSUMER ADVOCATE:
20	L. Vincent Williams, Esq.
	Consumer Advocate
21	1504 Parkway Towers 404 James Robertson Parkway
22	Nashville, Tennessee 37243-0500
23	Steven A. Hart, Esq.,
<b>5</b> /	Special Counsel 450 James Robertson Parkway
2 4	Nashville, Tennessee 37243-0485
25	MARV

Docket No 97-00982 Exhibit CA-SNB\_\_\_\_

Docket No 97-00982
Exhibit CA-SNB\_\_\_\_
Direct Testimony\_\_
Schedule 7\_\_\_\_
Page 2 of 2

1 dividends --

A Where are we?

Q I'm sorry, I've got the wrong page citations here. You can tell me whether you remember saying this or not. I can't find it through your testimony right now. In the case of public utilities dividends paid are constant for certain periods and are increased at irregular intervals even though financial processes underlying their movement may be progressing much more smoothly and constantly; does that sound correct?

A I think I would say smoothly and continuously, but whatever, but yes, that is true.

- Q Do you agree --
- A It's true as a general rule.
- Q So you would agree that a public utility and natural gas public utility, their financial activity is basically smooth and continuous?

A Well, what I said, I think if we had the complete quotation would be that earnings and cash flows progress smoothly and continuously. Financial processes occur smoothly and continuously. They go -- if this makes the point for you -- minute by minute, hour by hour, day by day and they're not interruptable.

Q Just to clarify for the record we found the first segment that we didn't really dispute. It starts

## CAPITAL STRUCTURE SUBMITTED IN DOCKET 95-02116

AS EXHIBIT 3 SCHEDULE 9

Docket No 97-00982							
Exhibit CA-SNB							
Direct Testimony							
Schedule 8							
Page 1 of 1							

CHATTANOOGA GAS COMPANY Cost of Capital For the 12 Months Ending September 30 1996

Line No		Amount	Ratio	Cost	Weighted Cost
1	Short Term Debt	5 190 953	5 36%	8 00%	0 43%
2	Long Teel Debt	43 096 531	44 50%	7 96%	3 54%
3	Preferred Stock	4 183 753	4 32%	7 56%	0 33%
4	Common Stock Equity	44 374 900	45 82%	12 50%	5 73%
5	Total ,	96 846 137	100 00%		10 03%

## DCF Recommended Return

Page 1 of 1	Schedule 9	Direct Testimony	Exhibit CA-SNB	COCKET IND
-	9	stimony	A-SNB	COCKEL NO. 31-00367

## DCF SUGGESTED RATE OF RETURN

5.17%	rield	Average Div. Yield	
5.19%	\$21	\$1 14	wasiington Gas Eight
4.84%	\$23.76	\$1.15	Washington Co. Light
5.42%	\$33.79	\$1 83	Piedmont
5.05%	\$23 77	\$1.20	Positos Positos
5.45%	\$23 11	\$1.26	
4.49%	\$24.70	\$1 11	lidala Eleigy
5.05%	\$28.14	\$1.42	Indiana Engage
5.61%	\$27.08	\$1.52 31.52	Brooklyn Union
5.40%	\$19.63	\$106	Atlanta Gas
Yield	closing Price:		
Annual Dividend	Average Daily	12/96. Annual Dividend	Company

AGL	Actual Value-Line Projection
AGL DIVIDEND GROWTH RATE	Year of AGL Dividend 1996 2000
5.23%	\$1.06 \$1.30

DCF Suggested Rate of Return

10.40%

7 948%	Average / Most Recent 12 Months				yle 1 35, line 38 )) and G13(415)	al Reserve Bulletin, Table A26 Subtable 1 35, line 38 Federal Reserve Publications H15(519) and G13(415)	Sources: Federal Reserve Bulletin, Table A26: Subtable 1:35, line 38 Federal Reserve Publications H15(518) and G13(415)	Source			
801%	Average	7 782%	Average	7 582%	Average	8 278%	Average	7 458%	Average	8 727%	Average
	Dec	7 63%	Dec	103	Sec.	3					•
	ş	7 54%	V	35	2 8	8 79 M	7	7 28%	D R	8 37 <b>%</b>	Dec
	õ	7 83%	: ជួ	7 30%	Z (	30 ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) (	Z	7 25%	Nov	8 58%	Nov
	, vep	000	. <del>2</del>	7 202	2 ;	8 80%	8	0.91%	9	0.04%	: <u>G</u>
	8	70/3	2	7 5 5 6	§ .	8 62%	န္	8 94¥	Ş	8.79	2 8
	. <u>.</u>	107	A 5	7 24 2	Aug :	8 36%	<b>&gt;</b>	7 18%	P.	8 85 %	
	Ę	813%	: <u>\$</u>	7 77%	E !	8 45%	בֿ	7 43%	Ē	8 8 4 %	ב ב
	May	8 20%	May	7 80	<b>j</b>	8 30%	Jun ,	7 58%	Š	8 70%	- E
8 23%	Apr	7 80%	Þ	7712	<b>E</b> 2	8 37%	May ?	7 75%	May	881%	May
8 08%	Mar	7 75%	Mar	5		A 70° A	A i	7 06%	À	8 87%	Apr
7 81%	Feb	7 31%	9	0 00%	F 6	7 82%	Mar	761%	X.	8 89%	Na.
7 93%	Jan 97	7 08%	DB-CEC	0 73 M		7 68	F.	7 80%	F.	8 83%	9
	1997	_	. 1986		120 Oct 1895				_	8 72%	Jan 92
				•	ŧ		1904		1983		1992

Direct Teathnory
Schedule 10
Page 1 of 1

# INION FIGHTIUM PAIA FOI LATHE COMPANIES: 1925-1996

ACTUAL RETURN	If \$1 Were Invested in 1925 and the Investment Grew by 10.7% Every Year, the Result Would Be \$1370.95.	
TURN	1929 1930 1931 1932 1932 1933  1988 1988 1988 1990 1991 1992 1993 1994 1995	YEAR (1) 1925 1926 1927
10 7%	2 02 1 52 0 86 0 79 1 21 	Large Company Total Return Index For Year (2) 1 00 1.12 1 54 2 20
12 7%	-8.44% -24.88% -43.34% -8.15% 53.87%	Year-To-Year Percentage Change in Large Company Total Return Index (3) 11.60% 37.54% 43.58%
BIASE		
BIASED RETURN	The Average Return, 12.7%, Says the Wealth Accumulated Since 1925 should be \$4768. This is Inaccurate.	

\*Source: Ibbotson Associates 1997 Yearbook:

Column (2) - From Table B-1 Column (3) - From Table A-1

Exhibit CA-SNB
Direct Testimony
Schedule 11
Page 1 of 1

The Table Below Shows The Odds In 1996 Of Achieving The Actual Return And The Biased Average Return From A \$1 Investment In 1925 In A Large Company

ODDS OF

		BIASED AVERAGE	ACTUAL RETURN		
1 0E+0	158 5E+18 126 8E+18 95 8E+18 68 5E+18 46 2E+18 29 4E+18 17 6E+18 10 0E+18	221 3E+18 209 3E+18 187 3E+18	46 2E+18 68 5E+18 95 8E+18 126 8E+18 158 5E+18 157 3E+18 209 3E+18 221 3E+18	(1) 1 0E+0 71 0E+0 2 5E+3 57 2E+3	NUMBER OF POSSIBILITIES
\$854,908,330	\$5,109 \$7,440 \$10,835 \$15,778 \$22,977 \$33,460 \$48,727 \$70,959	\$1,654 \$2,409 \$3,508 \$4,768.40	\$82 \$119 \$173 \$253 \$368 \$536 \$7,80 \$1,136 \$1,136	(2) \$0 00 \$0 00 \$0 00 \$0 00	ALL POSSIBLE VALUES OF
33 6%	12 8% 13 4% 14 0% 14 6% 15 2% 15 8% 16 4% 17 0%	11 0% 11 6% 12 2% 12.7%	6.4% 7.0% 7.5% 8.1% 8.7% 9.3% 9.8% 10.4%	(3) -8 3% -7 8% -7 3% -6 8%	ALL POSSIBLE RETURNS
0%	7% 5% 4% 1% 1% 0%	9% 8%% 7%	2% 3% 5% 5% 7% 9%	(4) 0% 0% 0%	ACHIEVING A RETURN EXACTLY EQUAL TO THE RETURN IN COLUMN (3)
100%	76% 83% 86% 92% 95% 97% 98%	50% 59% 68%	3% 5% 8% 12% 17% 24% 32% 41%	0% 0% 0%	ODDS OF ACHIEVING A RETURN LESS THAN THE RETURN IN COLUMN (3)
%0	12% 8% 5% 3% 2% 1% 0%	41% 32% 18%	95% 92% 88% 88% 68% 59% 50%	(6) 100% 100% 100%	ODDS OF ACHIEVING A RETURN MORE THAN THE RETURN IN COLUMN (3)

Direct Testimony
Schedule 12
Page 1 of 1

### Odds That A Large Company Has Achieved A Return Greater Than The Return At The Bottom Of This Chart

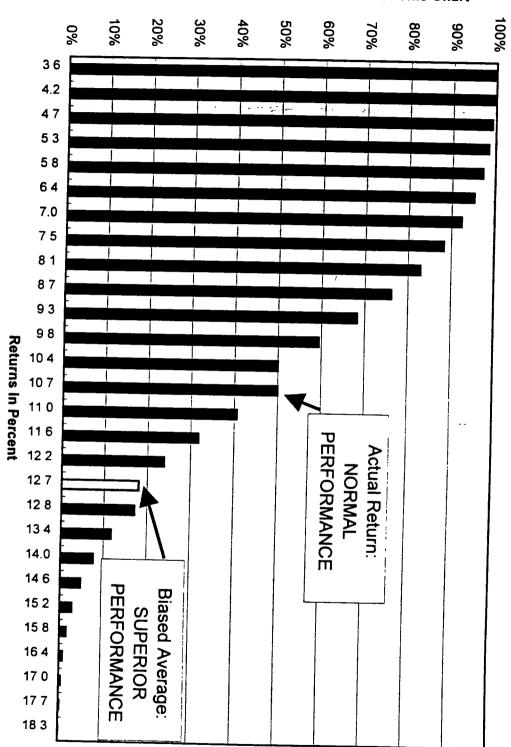


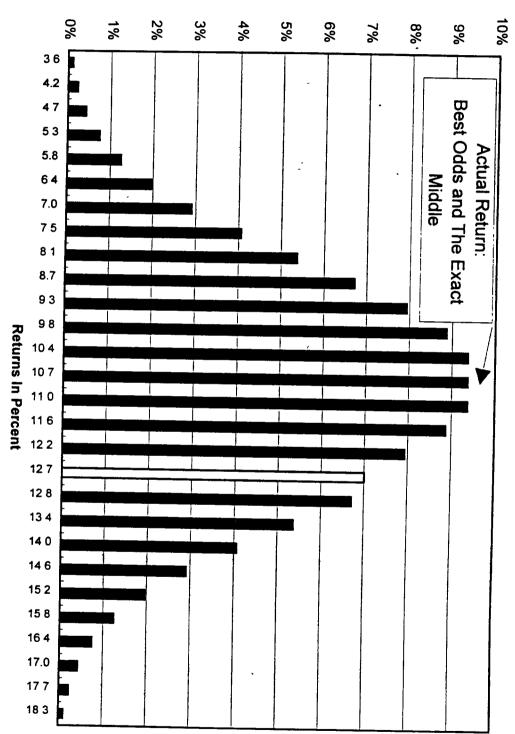
Chart 2

THE CUMULATIVE PROBABILITY DISTRIBUTION FOR IBBOTSON'S RETURNS

TO LARGE COMPANY STOCKS

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Chart 2 of 3

## Odds That A Large Company Has Achieved A Return Exactly Equal To The Return At The Bottom Of This Chart



## THE PROBABILITY DISTRIBUTION FOR IBBOTSON'S RETURNS TO LARGE **COMPANY STOCKS**

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Chart 3 of 3

\*Source Ibbotson Associates 1997 Yearbook Column (2) - From Table B-5 Column (3) - From Table A-14

Column (5) - From Table B-5 Column (6) - From Table A-14

Average Return

Ave	3 79%	3 74%	Actual Return			
-	5 21%	13 54000	1996	2 68%	1 57100	1960
-	561%	12 87000	1995	2 96%	1 53000	1959
-	391%	12 18600	1994	1 50%	1 48600	1958
-	2 90%	11 72800	1993	3 17%	1 46400	1957
-	351%	11 39800	1992 -	2 45%	1 41900	1956
-	5 59%	11 01200	1991	1 54%	1 38500	1955
-	7 82%	10 42900	1990	0 89%	1 36400	1954
-	8 37%	9 67300	1989	181%	1 35200	1953
•	6 35%	8 92600	1988	1 68%	1 32800	1952
•	5 47%	8 39300	1987	1 48%	1 30600	1951
•	6 16%	7 95800	1986	1 18%	1 28700	1950
•	7 72%	7 49600	1985	1 11%	1 27200	1949
•	9 85%	6 95900	1984	0 80%	1 25800	1948
-	881%	6 33500	1983	0 48%	1 24800	1947
•	10 54%	5 82200	1982	0 40%	1 24200	1946
•	14 70%	5 26700	1981	0 32%	1 23700	1945
•	11 24%	4 59200	1980	0 33%	1 23300	1944
•	10 37%	4 12800	1979	0 33%	1 22900	1943
•	7 19%	3 74000	1978	0 25%	1 22500	1942
•	5 12%	3 48900	1977	%80 O	1 22200	1941
•	5 06%	3 31900	1976	%00 0	1 22100	1940
•	5 79%	3 15900	1975	%00 0	1 22100	1939
•	8 03%	2 98600	1974	0 00%	1 22100	1938
•	6 92%	2 76400	1973	0 33%	1 22100	1937
•	3 82%	2 58500	1972	0 16%	1 21700	1936
-	4 40%	2 49000	1971	0 16%	1 21500	1935
_	6 52%	2 38500	1970	0 17%	1 21300	1934
-	6 57%	2 23900	1969	0 33%	1 21100	1933
<b>-</b>	5 21%	2 10100	1968	0 92%	1 20700	1932
•	4 23%	1 99700	1967	1 10%	1 19600	1931
J- 1	4 76%	1 91600	1966	2 42%	1 18300	1930
-	3 92%	1 82900	1965	471%	1 15500	1929
J- (	3 53%	1 76000	1964	3 57%	1 10300	1728
J- C	3 16%	1 70000	1963	3 10%	1 06500	1927
,-	2 74%	1 64800	1963	3 30%	1 03300	1926
-	2 10%	1 60400	1961		1 00000	1925
	(6)	(5)	(4)	(3)	(2)	3
	index	For Year	YEAR	Index	For Year	/EAR
3	Return	Index		Return	index	
	Total	Return		Total	Return	
	T-Bill	Total		T-Bill	Total	
<u>=</u> (	Change in	T-B <sub>ill</sub>		Change In	T-B#	
ř	Percentage			Percentage		
<b>Year</b>	Year-To-Year			Year-To-Year		

Exhibit CA-SNB
Direct Testimony
Schedule 13
Page 1 of 1

# Debt Instruments: Actual and Average Returns

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 14
Page 1 of 1

Returns of Debt Instruments 1925-1996

∪ S. Treasury Bills	Intermediate Term Government Bonds	Income Portion of Long-Term Government Bonds	Long-Term Government Bonds	Long-Term Corporate Bonds	
3 70%	5 20%	5.10%	5 10%	5 60%	Actual
3 80%	5 40%	5.20%	5.40%	6 00%	Biased Average

\*Source: Ibbotson Associates 1997 Yearbook Page 118

9370	0 368 0 434	0 848	0 241	0 283	0 333	0 677	0.420	0.25.0	STOCK IN THE STOCK
				} } !					AV BECENT 12 MTHS
Š		000	i						
5			0 118	297	0 464	0 677	0 383	0 506	/8-xdv
		0 886	0 311	0 427	0 503	0717	0 386	0.408	38-97
		0 912	0 361	0 368	0 475	0 735	0 393	2 4 5 4	No. 97
		0 915	0 358	0 364	0481	16.70	925	0 430	Feb. 97
		0 977	0 287	0 323	0 450	0 886	0 207	0.00	Jan-97
0 515	0 333 0	0 773	0 100	0 198	0 2/2	0 703	0.420	0.517	Dec. 96
		0 785	0 185	0 189	01/1	0.523		0.50	Nov-96
		0 781	0 158	0 205	01/0	0 0 0	0 4	0 0 0	00
		0 808	0 160		0 170	200		0.519	Sep-96
					0 178	0 661	0.422	0 590	Aug-96
		0 785	0 168	014	0 171	0 539	0 422	0 584	04-MC
		0 758	0 198	0 170	0 075	0 456	785.0	900	
		Ì	697.0	0 100	000				S S
		2		0 460	0.087	2	0448	0 532	May-96
	GAS LT CO GA	CORP	NAT GAS CO	6	INC.	GAS CO	001 01 000 00	5000	
PIEDMONT AVERAGE NATURAL FOR	_	ENERGY	NORTHWEST	LACLEDE GAS	INDIANA ENERGY LACLEDE GAS	BROOKLYN UN		ATLANTA GAS	BETA FOR 60 MONTH

RISK PREMIUM ANALYSIS BETAS — FOR AGL AND COMPARABLE COMPANIES REGRESSED AGAINST S&P 500

RISK PREMIUM ANALYSIS T-STATISTICS OF BETAS -- FOR AGL AND COMPARABLE COMPANIES REGRESSED AGAINST S&P 500

AV RECENT 12 MTHS	Apr-97	Mar-97	Feb-97	Jan-97	Dec-96	Nov-96	Oct-96	Sep-96	Aug-96	Jul-96	Jun-96	May-96	T-STATISTIC OF BETA FOR 60 MONTH PERIOD ENDING
2 3 16	2 208	2 087	1 842	1 813	2 113	2 321	2 428	2 355	2712	2 739	2 609	2 569	ATLANTA GAS LIGHT (ATG)
2 129	1 929	1 880	1 869	1 870	2 559	2 284	2 280	2 213	2 200	2 203	2 039	2 402	BAY ST GAS CO
3 188	3 286	3 435	3 438	3 442	3 935	3 417	3 005	2 935	2 525	2 463	2 073	2 305	BROOKLYN UN '
1 264	1 810	1 934	1 791	1 820	1 656	1 069	0 644	0 636	0 652	0 625	0 276	0 361	INDIANA ENERGY
1 554	2 591	2 362	2 035	2 025	1 670	1 094	1 036	1 129	0 831	0 764	0 897	0 930	LACLEDE GAS
1 248	1 761	1 612	1 829	1 821	1 406	0 522	0 958	0 828	0 871	0 874	0 988	1 463	NORTHWEST
3 379	3 435	3 482	3 515	3 525	3 747	3 189	3 223	3 184	3 261	3 231	3 064	3 222	PEOPLES ENERGY CORP
1 805	1 970	1 975	2016	2 006	2 035	1 720	1 689	1 678	1	1 468	2 110	2 276	WASHINGTON GAS LT CO
1 953		1 535	1 804	1 798	2 047	2413	2 044	2 033	2 152	2 160	1 791	1 875	PIEDMONT NATURAL GAS CO
2 093	2 282	2 256	2 238	2 236	2 352	2 003	1 923	1 888	1 856	1 836	1 761	1 934	AVERAGE FOR GROUP

RISK PREMIUM ANALYSIS ALPHAS – FOR AGL AND COMPARABLE COMPANIES REGRESSED AGAINST S&P 500

AV RECENT 12 MTHS	,	<b>≯</b> pr-96	Mar-96	Feb-96	Jan-96	Dec-95	Nov-95	Oct-95	Sep-95	Aug-95	Jul-95	Jun-95	May-95	ALPHA FOR 60 MONTH PERIOD ENDING
-0 002	,	-0 002	-0.001	5 60	5 66	5 6	-0.00	5 6	P 003	5 60	500	-0 003	-b 003	ATLANTA GAS LIGHT (ATG)
-0 001		5 6	8 2	5 5	8 5	3 5	3 5	3 5	8 5	3 2	2 6	0 000	0000	BAY ST GAS CO
-0 001	8	8 5	-002	683	- 003	602	600	9 5		8 8	2002	3 5	0.001	BROOKLYN UN GAS CO
0 003	6	0000	0000	-0 001	0000	0 001	0 004	0 004		000	0009		0 007	INDIANA ENERGY
0 002	6	-0 002	0001	000	0 002	0 002	0 002	0 003	0 004	0 003	0 003	3	3	LACLEDE GAS
0 001	0 002	0000	-0 001	0000	0 001	0 002	0 001	0 001	0 002	0 002	0 003			NORTHWEST
-0 004	-0 005	-0 005	-0 006	-0 006	-0 005	-0 00 <b>4</b>	-0 003	-0 003	-0 002	-0 003	-0 002	-0.003	}	PEOPLES ENERGY CORP
0 003	0 002	0 002	0 001	0 002	0 001	0 003	0 003	0 003	0 005	0 005	0 003	0 002	1	WASHINGTON GAS LT CO
0 002	0 002	0 002	0 000	0000	0001	0 001	0 002	0 002	0 002	0 002	0 005	0 004	!	PIEDMONT NATURAL GAS CO
0 000	-0 00 <del>1</del>	-b 001	-0 00 1	-0 00 <b>1</b>	-0 001	000	0 001	0 001	0 002	0 001	0 002	0 001		AVERAGE FOR GROUP

RISK PREMIUM ANALYSIS T-STATISTICS OF ALPHAS -- FOR AGL AND COMPARABLE COMPANIES REGRESSED AGAINST S&P 500

	AV RECENT 12 MTHS	Jun-96 Jul-96 Aug-96 Sep-96 Oct-96 Dec-96 Jan-97 Feb-97 Mar-97 Apr-97	T-STATISTIC OF ALPHA FOR 60 MONTH PERIOD ENDING May-96
	-0 355	-0 452 -0 408 -0 410 -0 323 -0 453 -0 355 -0 399 -0 358 -0 199 -0 378 -0 378	ATLANTA GAS LIGHT (ATG)
	-0 095	- 6 034 0 308 0 154 0 118 - 6 111 - 6 111 - 6 038 - 6 216 - 6 333 - 6 368 - 6 280	BAY ST GAS CO
	-0 117	0 131 0 289 0 032 0 258 -0 100 -0 206 -0 360 -0 500 -0 207 -0 310 -0 208	BROOKLYN UN GAS CO
	0 361	0 905 1 180 0 645 0 702 0 447 0 531 0 068 0 063 0 063 -0 141 0 036 -0 040 -0 059	INDIANA ENERGY
0323	200	0 697 0 815 0 632 0 785 0 620 0 420 0 407 0 421 0 089 -0 098 -0 293	LACLEDE GAS
0 189		0 083 0 488 0 324 0 322 0 172 0 189 0 388 0 181 -0 074 -0 165 0 076	NORTHWEST
0 540		-0 447 -0 324 -0 486 -0 287 -0 381 -0 437 -0 437 -0 497 -0 717 -0 822 -0 738 -0 659 -0 685	PEOPLES ENERGY CORP
0 426		0 337 0 508 0 822 0 902 0 466 0 473 0 439 0 152 0 270 0 171 0 309 0 267	WASHINGTON GAS LT CO
0 304		0 577 0 705 0 335 0 335 0 302 0 346 0 360 0 215 0 082 0 087 0 087 0 014	PIEDMONT NATURAL GAS CO
0 055		0 200 0 373 0 228 0 313 0 111 0 011 0 099 0 0119 0 0119 0 0199 0 164 0 183 0 130	AVERAGE FOR GROUP

Docket No 87-00982
Ezhibit CA SNB
Direct Testimony
Schedule 15
Page 4 of 4

# Risk Premium Suggested Rate Of Return

Page 1 of 1	Schedule 16	Direct Testimony	Exhibit CA-SNB	Docket No 97-00982

** Av of Comparable Cos	GAS CO	LT CO PIEDMONT NATURAL	CORP WASHINGTON GAS	GAS CO PEOPLES ENERGY	NORTHWEST NAT	INC	CO INDIANA ENERGY	BROOKLYN UN GAS	INC (HLDG CO)	AGL RESOURCES	COMPANY	
7 95%	7 95%	7 95%	7 95%	7 95%	7 95%	7 95%	7.95%	7 95%	7 95%		(a)	Debt
0 458	0 434	0 368	0 848	0 241	0 283	0 333	0 677	0 420	0 520		(b)	Beta
6 97%	6 97%	6 97%	6 97%	6 97%	6 97%	6 97%	6 97%	6 97%	6 97%		(c) (c)	Market Risk Premium =
0 032	3 02%	2 57%	5 91%	1 68%	1 98%	2 32%	4 72%		3 62%		Premium (d)=(b)X(c)	Company Risk
11 14%	10 97%	10 51%	13 86%	9 63%	9 92%	10 27%	12 67%	10 88%	11 57%		Cost (e)=(a)+(d)	Company Equity

\*\*Average Includes All Betas for All Companies Because the Average T-Statistics Are Greater Than 1 T-Statistics Are Shown In The Pnor Schedule

Risk Premium Suggested Rate Of Return

11.14%

## Any Model Kelying on Ibbotson's Data **Uses Monthly Compounding**

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 17

Page 1 of 1\_

lbbotson's Annual Returns Are Based on Monthly Compounding

12		ב ב	<del>)</del> «	α	· ~	1 O		<b>4</b> r	. c	) N	) <u> </u>		ROW		
12/1/96	11/1/96	10/1/96	9/1/96	8/1/96	//1/96	6/1/96	5/1/96	4/1/96	3/1/96	2/1/96	1/1/96			(1)	Month
-1 96%	7.59%	2.74%	5.62%	2.12%	-4 45%	0.41%	2 58%	1.47%	0 96%	0.96%	3.44%	•		(2)*	Monthly Return
98 04%	107.59%	102 74%	105 62%	102.12%	95.55%	100.41%	102.58%	101.47%	100 96%	100 96%	103 44%	100 00%		(3)	Monthly Return Relative to the Value "1"
123.07%	125 53%	116 68%	113 57%	107 52%	105 29%	110 20%	109.75%	106.99%	105 44%	104.43%	103 44%		col (3) x prior entry in col (3)	<b>(4)</b>	Cumulative Return in the Year Relative to the Value "1"
23.07%	25 53%	16.68%	13 57%	7 52%	5 29%	10.20%	9.75%	6 99%	5 44%	4.43%	3.44%			(5)	Cumulative Return in the Year

<sup>\*</sup>Source: Ibbotson Associates 1997 Yearbook Page 181, Table A-1 for 1996

Docket N	lo. 97-00982
Exhibit C	A-SNB
Direct Te	stimony
Schedule	18
Page 1 d	

### CHATTANOOGA GAS COMPANY

Office of the Consumer Advocate Interrogatory/Data Request - June 4, 1997

Item 42

- 42. Q. With regard to Exhibit 5 Schedule 9 of the company's filing, show the calculations and provide the data used to develop the figures shown under the column headings "Amount", "Ratio" and "Cost".
  - A. See attached documentation.

Docket No. 97-00982 Exhibit CA-SNB\_\_\_\_\_ Direct Testimony

AGL Resources
Projected Capitalization Ratios

2 - Court Court	nony_
Schedule 18	, '
D- 1000	
Page 2 of 2	
0 0. 2	

0h-49 -	1997	1998	Average	Date
Short Term Debt Long Term Debt Preferred Stock Common Stock Equity		,	75,579 659,500 64,280 632,102 1,431,461	Ratio 5.28% 46.07% 4.49% 44.16% 100.00%

## Chattanooga Gas Company Test Year Projected Capitalization

Short Term Debt Long Term Debt Preferred Stock Common Stock Equity	Ratio 5.28% 46.07% 4.49% 44.16% 100.00%	Amount 5,060,518 44,154,936 4,303,357 42,324,333 95,843,144
---	--	--

## AGL Resources Projected Cost of Capital Components

Long Term Debt	
Projected Balance	659,500,000
Less: Unamortized Loss on Repurchase	1,585,136
Less: Unamortized Debt Discount & Evpanse	3,702,500
Net Projected Balance	654,212,364
Projected Interest Cost	
Projected Cost Rate	50,730,000 7.75 <b>%</b>
Short Term Debt	
Projected Average Monthly Balance	40.000
Projected interest Cost	49.900,000
Projected Cost Rate	2,892,000 5.80%
Preferred Stock	3.50%
Projected Balance	64,280,000
Projected Dividend Accrual	4.525,000
Projected Cost Rate	7.04%
Common Stock Equity	
Projected Cost Rate	
See Cost of Equity Testimony & Exhibits	12 25%

## **Recommended Over All Return**

	Ratio	Cost	Weighted Cost
Short-Term Debt	5 28%	5 80%	0.31%
Long-Term Debt	46 07%	7 75%	3 57%
Preferred Stock	4 49%	7.04%	0.32%
Common Equity	44 16%	10 55%	4.66%
Total	100.00%		8 85%

ယ

N

G

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 19
Page 1 of 1

# Data on Mutual Funds Specializing in Small Company Stocks; 5-31-97

r ainstoile Siliaii Cap Insti	Parketone Small Co. Latt	IBM Discrete Cap Growth Admin	PIMCo Small Cap Value Admin	PIMCo Small Cap Value Insti	Hancock Small Cap Equity	Emeraid Small Cap Insti	I CW Galileo Small Cap Growth	Nations Small Cap Gr Prim A	Compass Small Cap Val Instl	Compass Small Cap Grth Insti	Munder Small Company Grth Y	Enterprise Small Co Value Y	First Harrord Small Company Y	Lazard Inti Smail Cap Insti	Crappe Huson Small Cap Insti	JPM Insti U.S. Small Company	Lazard Small Cap Insti	DFA Intl Small Cap Value	DFA U.S. 9-10 Small Company	DEA U.S. 6-10 Small Company	DFA Continental Small Compny	DFA Pacific Rim Small Compny	DFA Japanese Small Company	DFA U.S. Small Cap Value	DFA United Kingdom Small Co	Bear Stearns Small Cap Val Y	Benchmark Small Co Index A	UAM ICM Small Company	GMO Small Cap Value III	PIMCo Small Cap Growth Inst!	Pioneer Small Company C	Pioneer Small Company B	Pioneer Small Company A	Artisan Small Cap	MFS Aggr Small Cap Eq A	Montgomery Small Cap R	MAS Small Cap Value	Rowe Price Small-Cap Val	Standish Small Cap Equity		Company name	
Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Foreign Stock	Small Company	Small Company	Small Company	Foreign Stock	Small Company	Small Company	Europe Stock	Pacific Stock	Pacific Stock	Small Company	Europe Stock	Small Company	Small Company	Small Company	Growth	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company		Objective	
PKSCX	PPCAX	n/a	n/a	PSVIX	n/a	EMSCX	n/a	PSCPX	PNSEX	PSGIX	WULYX	EIGYX	n/a	LZISX	CHISX	XSSUL	LZSCX	DISVX	DFSCX	DFSTX	DFCSX	DFRSX	DFJSX	DFSVX	DFUKX	BSVYX	BSCAX	ICSCX	GMSVX	PSCIX	PCSCX	PBSCX	PSCFX	ARTSX	MASCX	MNSCX	MPSCX	PRSVX	SDSCX		Ticker	
\$100,000	\$100,000	\$200,000	\$200,000	\$200,000	\$250,000	\$250,000	\$250,000	\$500,000	\$500,000	\$500,000	\$500,000	\$1,000,000	\$1,000,000	\$1,000,000	\$1,000,000	\$1,000,000	\$1,000,000	\$2,000,000	\$2,000,000	\$2,000,000	\$2,000,000	\$2,000,000	\$2,000,000	\$2,000,000	\$2,000,000	\$2,500,000	\$5,000,000	\$5,000,000	\$35,000,000	\$Closed	\$Closed	\$Closed	\$Closed	\$Closed	\$Closed	\$Closed	\$Closed	\$Closed	\$Closed		Minimum Initial Purchase	
11 45	9 63	11 41	9 19	9 19	12 49	10 14	108	9 34	8 25	11 64	11 25	7 81	0	162	3 97	96	8 3	10 57	8.75	9 11	14 28	25 72	4 35	7 01	19 98	7 57	9 37	8 89	0	11 07	5 07	5 07	5 07	10 68	14 24	12 11	9 47	10 36	9 51	;	Return on Assets %	
27 7	20 75	16 71	27 37	27 72	13 48	10 69	17 54	20 72	19 87	31 58	37 17	11 83	n/a	15 65	n/a	20 84	23 93	0 95	17 65	17 68	14 32	14 36	-22 78	22 33	29 81	15 87	15 97	23 01	20 16	16 83	n/a	23 21	24 15	11 86	15 45	18 69	35 15	24 61	17 36	;	96 Rtrn %	

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 20
Page 1 of 6

# שמום סוו mutual Funds Specializing in Small Company Stocks; 5-31-97

Docket No 97-00982
Exhibit CA SNB
Direct Testimony
Schedule 20
Page 2 of 6

Scudder Small Company Value	BT Investment Small Can	Galaxy Small Co Equity Bet A	Rowe Price Small Cap Stk	Vista Small Cap Equity B	Vista Small Cap Equity A	Galaxy II Small Co Index Ret	Vanguard Index Small Cap Stk	PBHG Strategic Small Co PBHG	rocqueville Small Cap Val A	Prudential Small Companies C	Compass Small Cap Val Svc	Compass Small Cap Grth Svc	Stratton Small-Cap Yield	Brazos/JMIC Small Cap Growth	RCM Small Cap	CRM Small Cap Value	LRCM Small Cap Equity	LKCM Small Cap Equity	Longleaf Partners Small-Cap	Hotchkis & Wiley Small Cap	Quaker Small-Cap Value	UAM FMA Small Company	Schroder Small Cap	larget Small Cap Growth	Target Small Cap Value	Glenmede Small Cap Equity	Rainier Small/Mid Cap Equity	Pictet Intl Small Companies	DLB Global Small Cap	SEI Insti Small Cap Value A	59 Wall St Small Company	SEI Insti Small Cap Growth A	SEI Insti Sn'all Cap Growth A	Kent Small Co Growth Insti	Berger Small Cap Value Inst	Avesta Small Capitalization	lurner Small Cap Equity	Standish Small Cap Tax-Sen	Company name	
Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Growth	Foreign Stock	World Stock	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Objective	
SCSUX	GASEX	DSCVX	OTCFX	VSEBX	VSEAX	ISCIX	NAESX	PSSCX	TSCVX	n/a	PSESX	PCGEX	STSCX	BJSCX	n/a	CRMSX	LKSCX	LKSCX	LLSCX	HWSCX	n/a	<b>FMACX</b>	WSCVX	TASGX	TASVX	GTCSX	RIMSX	PTSCX	DLBSX	SESVX	FNSMX	SSCGX	SSCGX	KNEEX	OMNIX	n/a	TSCEX	SDCEX	Ticker	
\$2,500 \$2,500	\$2,500	\$2,500	\$2,500	\$2,500	\$2,500	\$2,500	<b>\$</b> 3,000	\$5,000	<b>\$</b> 5,000	<b>\$</b> 5,000	<b>\$</b> 5,000	\$5,000	\$5,000	\$10,000	\$10,000	\$10,000	\$10,000	\$10,000	\$10,000	\$10,000	\$25,000	\$25,000	\$25,000	\$25,000	\$25,000	\$25,000	\$25,000	\$100,000	\$100,000	\$100,000	\$100,000	\$ 100,000	\$100,000	\$100,000	\$100.000	\$100,000	\$100,000	\$100,000	Purchase	Minimum Initial
11 18 8 61	11 05	7 65	10 41	104	10 4	10 27	9 32	0	9 78	9 09	8 25	11 64	97	0	971	5 46	861	861	8 12	9 34	0	8 52	8 92	12 36	9 17	9 33	9 37	14 65	15 07	œ ;	10 42	10 0	10 95	20 I	8 2 B	10 78	11 24	1 26	Assets %	Det im on
6 9 23 84	20 84	34 15	21 05	27 93	28 8	19 66	18 12	n/a	25 03	22 97	19 56	31 39	14 97	n/a	34 41	38 95	26 95	26 95	30 64	14 27	n/a	26 2	23 91	18 88	21 84	25 1	22 56	n/a	58.6	22 13 23 13	19 13	19 14	1914	10.61	25 G	30 95	28 85	21 23	% % S	

# Data on Mutual Funds Specializing in Small Company Stocks; 5-31-97

Kemper-Ureman Small Cap A	Munder Small Company Grth B	Munder Small Company Grib C	Norwest Advant Small Cap I	Muliuer Small Company Grth A	Accessor small to Mid Cap	Assem Small Cap Growth	Goball Sacris Small Cap Eq 8	Goldman Sachs Small Cap Eq A	Westcore Small-Cap Opport	Markstone Small Cap Inv B	Parkstone Small Cap Inv C	Heritage Small Cap Stock C	Parkstone Small Cap Inv A	Heritage Small Cap Stock A	Colonial Small Cap Value B	Colonial Small Cap Value A	Norwest Advant Small Co Gr I	rederated Intl Small Co C	recerated Inti Small Co B	recerated Small Cap Strat C	Federated Small Cap Strat B	Berger Small Company Growth	Fremont Intl Small Cap	Clover Capital Small Cap Val	Rembrandt Small Cap Inv	Crabbe Huson Small Cap Prim	FBR Small Cap Growth/Value	FBR Small Cap Financial	Columbia Small Cap	AARP Small Company Stock	Sit Small Cap Growth	Bridgeway Ultra-Small Co	PIC Small Cap Growth	Fidelity Japan Small Co	Strong Small Cap	Northern Small Cap	Fidelity Small Cap Stock	Galaxy Small Cap Value Ret A	Warburg Pincus Small Val Com		Company name
Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Foreign Stock	Foreign Stock	Small Company	Small Company	Small Company	Foreign Stock	Small Company	Small Company	Small Company	Small Company	Sp -Financial	Small Company	Small Company	Small Company	Small Company	Small Company	Pacific Stock	Small Company	Small Company	Small Company	Small Company	Small Company		Objective
KDSAX	MULBX	n/a	NVSOX	MULAX	ASMCX	GABSX	GSQBX	GSSMX	WTSCX	PKSBX	n/a	HSCCX	PKSAX	HRSCX	CSSBX	CSMIX	NVSCX	ISCCX	ISCBX	SMCCX	SMCBX	BESCX	FRISX	n/a	n/a	CHSCX	n/a	n/a	CMSCX	ASCSX	SSMGX	BRUSX	PISCX	FJSCX	SCAPX	NOSGX	FDSCX	SSCEX	WPSVX		Ticker
\$1,000	<b>\$</b> 1,000	<b>\$1</b> ,000	<b>\$</b> 1,000	<b>\$1</b> ,000	<b>\$1</b> ,000	<b>\$1</b> ,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	<b>\$</b> 1,000	<b>\$</b> 1,000	\$1,000	<b>\$1</b> ,500	<b>\$1</b> ,500	\$1,500	<b>\$1</b> ,500	<b>\$</b> 2,000	<b>\$</b> 2,000	<b>\$</b> 2,000	\$2,000	\$2,000	\$2,000	\$2,000	\$2,000	\$2,000	\$2,000	\$2,000	\$2,000	\$2,500	\$2,500	\$2,500	<b>\$</b> 2,500	\$2,500	<b>\$</b> 2,500	חוכומשם	Minimum Initial
8 94	11 25	11 25	0	11 25	11 8	7 54	6 13	6 13	8 28	11 45	11 45	11 71	11 45	11 71	11 02	11 02	8 48	13 73	13 73	13 04	13 04	11 14	11 81	5 92	13 ် 9	3 97	16 61	<b>D</b> O	ဖ	0	12 65	10 44	11 78	7 67	10 12	6 92	11 18	9 2 1	8 52	Assets %	Return on
296	35 9	36 23	n/a	36 83	24 74	11 88	n/a	21 84	25 58	<b>26 62</b>	26 24	26 45	27 59	27 46	17 84	18 35	19 82	n/a	n/a	33 99	34 16	16 77	12 15	n/a	19 18	n/a	n/a	n/a	n/a	n/a	14 97	29 74	18 7	-24 59	227	18 93	13 63	26 84	56 2	8	96 Rtrn

٢

Docket No 97 00982
Exhibit CA SNB
Direct Testimony
Schedule 20
Page 3 of 6

1			Minimum Initial	Return on	QS RITE
company name	Objective	Ticker	Purchase	Assets %	%
ESC Strategic Small Cap A	Small Company	ESCAX	\$1,000	0 67	3
Kemper-Dreman Small Cap C	Small Company	KDSCX	\$1,000	10	20 04
Kemper-Dreman Small Cap B	Small Company	KDSBX	\$1,000	8 94 8 94	28 54
ESC Strategic Small Cap D	Small Company	ESCDX	\$1,000	967	26 83
SogA Small Cap	Small Company	SVSCX	\$1,000	11 43	28 79
Bear Stearns Small Cap Val A	Small Company	BSVAX	\$1,000	7 57	15 43
BBST Small Cap Val C	Small Company	BSVCX	\$1,000	7 57	14 83
BRAT Small Company Growth A	Small Company	BBBSX	\$1,000	11 59	30 77
Montgomen, but Small Car D	Small Company	n/a	\$1,000	11 59	30 98
Oakmark Small Cap K	Foreign Stock	MNISX	\$1,000	23 45	14 97
Kent Small Co Croude Incom	Small Company	OAKSX	\$1,000	8 82	39 79
TCW/DW Small Can Growth	Small Company	KNEMX	\$1,000	8 95	19 15
Invesco European Small Co	Firone Stock	IVECY	\$1,000	11 33	13 71
Harris Ins Small-Cap Instl	Small Company	HSCIX	\$1,000	10.67	31 03
Harris Ins Small-Cap A	Small Company	n/a	\$1,000	10.57	n/3
HSBC Small Cap	Small Company	MSCFX	<b>\$1</b> ,000	119	15 29
Schuch Small Companies A	Small Company	PGOAX	<b>\$</b> 1,000	9 09	23 92
SEI Inst Small Can Growth D	Small Company	SWSMX	\$1,000	9 72	15 49
PIMCo Small Can Value A	Small Company	n/a	\$1,000	10 96	18 75
PIMCo Small Cap Value B	Small Company	PCVAX	\$1,000	0	n/a
PIMCo Small Cap Value C	Small Company		41,000	· c	n/a
Pegasus Small Cap Opport I	Growth	PSOPX	\$1,000	10 FG	n/a
Pegasus Small Cap Opport A	Growth	n/a	\$1,000	5 6	24 50
Pegasus Small Cap Opport B	Growth	n/a	\$1,000		24 42
Francial Small Companies B	Small Company	CHNDX	\$1,000		22 97
Value Line Small Cap Eq Inc Y	Small Company	ESCEX	\$1,000	_	22 38
Evergreen Small Cap Ed Inc. A	Small Company	VLSCX	\$1,000		10 35
Evergreen Small Can En Inc B	Small Company	n/a	\$1,000		22 01
Evergreen Small Cap Eq Inc C	Small Company	n/a	\$1,000		21 1
Norwest Advant Small Co StkA	Small Company	NCSAX	\$1,000	12 77	)E 08
Norwest Advant Small Co Stkl	Small Company	NSCTX	\$1,000		26 03
Arch Small Co. StkB	Small Company	NCSBX	\$1,000		24 91
Investo Small Cap Equity Inv A	Small Company	<b>EMGRX</b>	<b>\$1</b> ,000		10.5
Preferred Small Can	Small Company	IDSCX	\$1,000		12 46
Heartland Small Can Contrar	Small Company	PSMCX	\$1,000	11 78	20 46
Arch Small Cap Equity Inv B	Small Company	HRSMX	\$1,000		18 86
	Office Company	n/a	\$1,000	9 87	9 82

٦

Docket No 97 00982
Exhibit CA SNB
Direct Testimony
Schedule 20
Page 4 of 6

# Data on Mutual Funds Specializing in Small Company Stocks; 5-31-97

receiated inti Small Co A	Endorsted Lating Small Cap Eq	DIMO Maria Comps Val C	Cualinast Small Camp Valo	Change Small Comps Val A	Outsined Small Cap Strat A	Enderstad Small Cap A	Phone Small Cap Val INV A	Compass Small Cap Grin Inv A	Compass Small Car Car II	SinAmerica Small Co Grin A	Sun America Small Company B	Senting Small Company A	Sortion Small Cap Equity C	Nemper Small Cap Equity B	Enterprise Small Co Value B	nemper small Cap Equity A	Enterprise Small Co Value A	Neystone Small Co Grth (S-4)	Cean Witter Intl Small Cap	Neysione Small Co Grth II C	Neystone Small Co Grth II B	Keystone Small Co Grth II A	Emerald Small Cap Ret	Marshall Small-Cap Growth	IT I Hartford Small Company B	IT I Hartford Small Company A	AAL Small Cap Stock A	PaineWebber Small Cap C	PaineWebber Small Cap B	Eastcliff Regional Small Cap	PaineWebber Small Cap A	Safeco Small Co Stock NoLoad	Aetna Small Company Adv	invesco Small Company Growth	Gateway Small Cap Index	Aetha Small Company Sel	North American Small/Mid B	North American Small/Mid C	North American Small/Mid A		Company name
Foreign Stock	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Aggressive Growth	Foreign Stock	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Growth	Growth	Growth		Objective
ISCAX	RISCX	n/a	PHSCX	QSVAX	SMCAX	PHSAX	PSEIX	CSGEX	SEGBX	SEGAX	n/a	SAGWX	KSCCX	KSCBX	ESCBX	KSCAX	ENSPX	KSFOX	DWISX	KSGCX	KSGBX	KSGAX	n/a	MRSCX	n/a	IHSAX	AASMX	PSCDX	PSCBX	EARSX	PSCAX	SFSCX	AESAX	FIEGX	GSCIX	AESGX	NSMBX	NSMCX	NSMAX		Ticker
\$500	\$500	<b>\$</b> 500	\$500	<b>\$</b> 500	\$500	\$500	<b>\$</b> 500	<b>\$</b> 500	\$500	<b>\$</b> 500	\$1,000	\$1,000	<b>\$</b> 1,000	<b>\$1</b> ,000	\$1,000	<b>\$</b> 1,000	\$1,000	<b>\$1</b> ,000	\$1,000	\$1,000	<b>\$1</b> ,000	\$1,000	\$1,000	\$1,000	<b>\$1</b> ,000	\$1,000	\$1,000	<b>\$1</b> ,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	\$1,000	<b>\$</b> 1,000		Minimum Initial Purchase
13 73	10 1	9 89	12 38	9 89	13 04	_	8 25	11 64	10 23	10 23	10 49	10 49	10 41	10 41	7 81	10 41	7 81	12 67	21 66	10 34	10 34	10 34	10 14	0	0	11 36	921	10 94	10 94	10 12	10 94	808 -	10 1	12 21	9 13	10 1	11 94	11 94	11 94		Return on
n/a	21 92	19 35	28 93	20 07	35 04	29 96	19 34	31 13	14 12	14 92	n/a	21 3	12 86	12 84	10 77	14 09	11 28	082	101	n/a	n/a	n/a	10 05	n/a	n/a	n/a	n/a	16 22	16.2	n/a	17 16	7/2	12 79	11 62	17 04	13 62	n/a	n/a	n⁄a	3	96 Rtrn %

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 20
Page 5 of 6

Ō
g
omaii
Company
Stocks; 5-31-97

Locket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 20
Page 6 of 6

Crown Capital Small Co Insti	nemper small cap Equity i	Seriost inv small Cap	Remorandt Small Cap Tr	Arch Small Cap Equity Insti	Arch Small Cap Equity Tr	Galaxy Small Cap Value Tr	Pacific Advisors Small Cap	Prudential Small Companies Z	Qualivest Small Comps Val Y	Warburg Pincus Adv Small Val	DFA U.S. Small Cap Value II	BB& Small Company Growth Tr	Galaxy Small Co Equity Tr	Aiger Small Cap Retirement	Landmark Small Cap Equity A	Munder Small Company Grth K	empleton Global Small Co II	l empleton Global Small Co I	Franklin Small Cap Grth II	Franklin Small Cap Grth I	Piper Small Company Growth A	Keeley Small Cap Value	Winthrop Small Company Val A	Alger Small Capitalization B	Alger Small Capitalization A	First Omaha Small Cap Value	GI Global Amer Small Cap B	GT Global Amer Small Cap A	GT Global Amer Small Cap Adv	ONE Fund Small Cap	Company name
Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	World Stock	World Stock	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Small Company	Objective
	n/a	n/a	RSMCX	n/a	n/a	SMCEX	PASMX	PSCZX	QSVYX	n/a	DFAVX	BBCGX	GSETX	ALSRX	LSCEX	MULKX	TESGX	TEMGX	FRSIX	FRSGX	PJSCX	KSCVX	WFAGX	ALSCX	n/a	n/a	GTSBX	GTSAX	n/a	n/a	Ticker
	\$0	<b>\$</b> 0	\$0	<b>\$</b> 0	\$0	<b>\$</b> 0	\$0	<b>\$</b> 0	<b>\$</b> 0	<b>\$</b> 0	<b>\$</b> 0	<b>\$</b> 0	<b>\$</b> 0	<b>\$</b> 0	<b>\$</b> 0	\$0	<b>\$</b> 100	<b>\$</b> 100	<b>\$</b> 100	<b>\$</b> 100	\$250	<b>\$2</b> 50	<b>\$</b> 250	\$500	<b>\$</b> 500	<b>\$</b> 500	<b>\$</b> 500	<b>\$</b> 500	<b>\$</b> 500	<b>\$</b> 500	Minimum Initial Purchase
10 44	10 41	9 56	139	9 87	9 87	9 21	10 89	9 09	9 89	8 52	7 01	11 59	11 05	12 02	9 44	11 25	18	18	10 31	10 31	92	7 83	96	12 59	12 59	8 52	8 85	8 85	8 85	9 34	Return on Assets %
	14 54	n/a	19 42	10 62	10 98	27 19	437	n/a	20 36	57	22 07	31 19	21 59	14 83	37 8	36 89	21 35	22 09	26 07	27 07	11 65	25 99	14 58	4 17	n/a	n/a	13 14	13 81	14 22	17 01	96 Rtrn %

### Morning Star Report on DFA 9-10 Fund

Docket No 97-00982
Exhibit CA-Sh'3\_\_\_
Direct Testimony\_
Schedule 21\_\_\_\_
Page 1 of 3\_\_\_\_

DFA U.S. 9-10 Small Company (Data as of 05-31-97)

Assets
Investment Objective Rating Load Yield (\$mil) NAV

Small Company \*\* None 0 21% 1107.8 11.65

DFA U.S. 9-10 Small Company Portfolio seeks long-term capital appreciation.

The fund invests in a diverse group of small companies with readily marketable securities. These companies may be traded on the NYSE, the AMEX, or the over-the-counter market, but their market capitalizations must be comparable with those in the smallest quintile of the NYSE. The portfolio is rebalanced at least semiannually.

The fund is designed primarily for institutional investors. Prior to April 10, 1989, the fund was named DFA Investment Dimensions Small Company. Prior to 1983, the fund was named DFA Small Company.

Performance: Annual Return %

YTD 1996 1995 1994 1993

DFA U S. 9-10 Small Company S&P 500 Index 4.02 17.65 34.48 3.09 20.97 15.43 22.95 37.53 1.32 10.06

These Figures Match DFA's and Dr. Andrews' Numbers in his Schedule 6, page 1, Far-left Column

Performance: Trailing Return %

3 Yr 5 Yr 1 Mo 3 Mo 1 Yr Avg Avg

DFA U.S 9-10 Small Company 10 22 1.92 -1.33 18 60 18 41 S&P 500 Index 6.08 7.80 29 40 25.92 18.36

Risk Measures

Morningstar Risk:

Above Avg.

Beta (3 Yr)

0 78

## Morning Star Report on DFA 9-10 Fund

Docket No 97-00982 Exhibit CA-SNB Direct Testimony Schedule 21 Page 2 of 3

Morningstar Return:

Average

Std. Deviation (3 Yr)

16 59

R-Squared

32

Top Ten Portfolio Holdings (Data as of 02-28-97)

	Amount		Value %	6 Net
Ticker	000	Security	\$000	Assets
KUH GLE INVX FRC ROG	117 179 157	Kuhlman Gleason Innovex First Republic Bancorp Rogers	 438 418 3844 345	7 0 36 4 0.33 3654 0.32
HEI CULP CDSI ELMG APR	179 105 142	HEICO Culp Computer Data Systems Electromagnetic Science American Precision Inds	3430 3214 es	0.00

Portfolio Statistics

Price/Earnings Ratio Price/Book Ratio.

21.64

Income Ratio %:

23 68

0 61

These figures are

Return on Assets %.

2 80

Turnover Ratio %:

the same as

Median Market Cap (\$mil) ₹ 123.29

8.75

Expense Ratio %.

those reported in DFA's 1996

This figure, 8.75%, is not provided in DFA's Annual Report See Schedule 22, page 2.

Annual Report

**Expenses and Fees** 

Front-End Load

0.00

12b-1 Fee:

0.00

Deferred Sales Charge:

0 00

Management Fee

0 50

Redemption Fee:

0.00

Operations

Ticker Symbol<sup>-</sup>

DFSCX

## Morning Star Report on DFA 9-10 Fund

Docket No 97-00982
Exhibit CA-SNB\_\_\_
Direct Testimony\_\_
Schedule 21 \_\_\_\_
Page 3 of 3\_\_\_\_

Fund Family:

**DFA Investment Dimensions Group** 

Address:

1299 Ocean Avenue 11th Floor

Santa Monica, CA 90401

Telephone:

310-395-8005

Fund Manager:

Management Team

Manager Tenure

NA years

Min. Initial Purchase \$2000000

(c)1997 Morningstar, Inc. All rights reserved 225 W. Wacker Dr. Chicago, IL 60606, 312-696-6000 Although data are gathered from reliable sources, completeness and accuracy cannot be guaranteed

Docket No. 97-00982
Exhibit CA-SNB\_\_\_
Direct Testimony\_\_
Schedule 22\_\_\_
Page 1 of 2\_\_\_\_

-

DFA Investment Dimensions Group Inc. and The DFA Investment Trust Company

## ANNUAL REPORT

Year Ended November 30, 1996

STATE OF THE WAS ASSESSED TO STATE OF THE PARTY OF THE PA

Docket No. 97-00982 Exhibit CA-SNB\_\_\_\_

Direct Testimony
Schedule 22
Page 2 of 2

## DFA INVESTMENT DIMENSIONS GROUP INC.

## FINANCIAL HIGHLIGHTS

## for a share outstanding throughout each year

New 30,   New							D MELEO OIL	THE CO. P. TO SHEW COMPANY PORTIONS	2				ļ
Net forcome From the Beginning of Period \$ 1103 \$ 849 \$ 869 \$ 775 \$ 633 \$ 534 \$ 574 \$ 776 \$ 5 6 7 9 9 8			Year Ended Nov 30, 1995	Year Ended Nov. 30, 1995	Year Ended Nov. 30, 1994	Year Ended Nov. 30, 1993	Year Ended Nov 30, 1992	Year Ended Nov. 30, 1991	Year Ended Nov 30, 1990	Year Ended Nov 30, 1969	Year Ended Nov 30,	Year En Nov 3 1983	\$ o. ~
Note   Personne Form   Perso		Net Asset Value Beginning of Period		\$ 8 49		\$ 775			\$ 774	\$ 766	2. 750	•	46
Nei Gan (Lossens) or Secures   165   261   040   167   153   164   (177)   098   148   1		Income From Investment Operations										]	i
Not Gable Coses)   168   2 66   0 40   167   153   164   (177)   0 99   149   168   140   168   140   168   140   168   140   168   140   168   140   168   140   168   140   168   140   168   140   168   168   140   168		Net investment income	0 03	900	0 0 1	0 03	00	30	0 0 0	0 0 0	010	0	60
Computed and Unrealized   188   261   040   167   153   164   (177)   098   148   168   178   168   (178)   168   158   158   168   (178)   168   158   158   158   (178)   168   158   158   158   (178)   168   158   158   158   (178)   168   15		Net Gain (Losses) on Securities											
Colai From Investment Operations   186   2 66   0 41   170   157   168   (170)   105   159   159   155   1		(Realized and Unrealized)	1 85		0 40	1 67	1 53	2	(177)	96 0	_		53)
Less Distributions   Correctioned		Total From Investment Operations	1 88		0 41	1 70	1 57	1 68	(1 70)	1 05	-	; =	3
Net five sine of forms (0 01) (0 04) (0 03) (0 05) (0 05) (0 05) (0 05) (0 05) (0 05) (0 05) (0 11) (0 12)		Less Distributions											
Not Realized Gains  Total Distributions  Net Asset Value, End of Period  S 12 14 \$  Total Return  Net Assets End of Period (thousands) \$1,181,804 \$5  Net Assets End of Period (thousands) \$1,181,804 \$5  Net Assets End of Period (thousands) \$1,181,804 \$5  Ratio of Represes to Average Net Assets  Assets Ratio of Net Investment Income to 0.22%  Portfolio Turnover Rate 23.66%  Average Commission Rate (1) \$0.0604  (1) Computed by dividing the total amount of brof ing the period for which commissions were ch		Net Investment Income	(00)	900	(0 03)	(0 02)	(0 02)	(0 0)	(80.09	(0.00)	9		١
Total Distributions   (0.77)   (0.12)   (0.61)   (0.76)   (0.15)   (0.68)   (0.70)   (0.97)   (1.42)		Net Realized Gains	(0 76)		0 20	(0.73)	0 0		(0 62)	0 88	(131)		ı
Net Asset Value, End of Period   \$ 1214		Total Distributions	(0 77)		(0 61)	(0 76)	(0 15)	ļ	(0 70)	(0 97)	1 42	1	
Total Return  Nel Assets End of Period (frousands) 81,181,804 8925,474 8659 221 8630,918 \$651,313 \$722,289 \$561,102 \$949,291 \$912,518 \$7  Nel Assets End of Period (frousands) 81,181,804 8925,474 \$659,221 \$650,918 \$651,313 \$722,289 \$561,102 \$949,291 \$912,518 \$7  Ratio of Nel Investment Income to 0.61% 0.62% 0.65% 0.70% 0.66% 0.64% 0.62% 0.62% 0.62% 0.62%   Average Nel Assets 23.66% 2.465% 16.56% 0.70% 0.65% 0.70		Net Asset Value, End of Period		\$ 11 03					1	1	\$ 766	-	18
Net Assets End of Period (thousands) \$1,181,804 \$925,474 \$659,221 \$630,918 \$651,313 \$722,289 \$561,102 \$949,291 \$912,518 \$7  Ratio of Expenses to Average Net Assets  Ratio of Net Investment Income to		Total Return	18 05%	3137%	5 08%	23 91%			(24 09)		24 36%	li	18
Assets  Raio of Net Investment Income to  Raio of Net Investment Income to  Raio of Net Investment Income to  0.22% 0.45% 0.16% 0.26% 0.53% 0.75% 0.89% 0.86% 1.19%  Raio of Net Investment Income to  0.22% 0.45% 0.16% 0.26% 0.53% 0.75% 0.89% 0.86% 1.19%  Raio of Net Investment to the Institution Info to the Information Info to the Information Info to the Information Info to the Information Info the period for which commissions were charged, as required by the SEC for fiscal years beginning after September 1, 1995	72	Nel Assets End of Period (thousands)	\$1,181,804	\$925,474	\$659 221	\$630,918	\$651,313	\$722,289	\$561,102	\$949,291	\$912,518	\$788	15
\$ 0.52% 0.45% 0.16% 0.26% 0.53% 0.75% 0.89% 0.86% 1.19% 23.68% 24.65% 16.56% 9.87% 9.72% 10.13% 3.78% 7.86% 25.98% 2 0.6504 N/A		Assels	0 61%	0 62%	0 65%				0 62%				61%
10 22% 0 45% 0 16% 0 26% 0 75% 0 75% 0 86% 1 19% 23 69% 24 65% 16 56% 9 87% 8 72% 10 13% 3 79% 7 86% 25 98% 2 24 65% 16 56% 9 87% 10 13% 3 79% 7 86% 25 98% 2 24 65% 16 56% 9 87% 10 13% 3 79% 7 86% 25 98% 2 25 9		Ratio of Net Investment Income to											:
10 (1) \$ 0.0604 NA N/A N/A N/A N/A N/A N/A N/A N/A N/A		Average Nel Assels	0 22%	0.45%	0 16%								95%
g the total amount of broi		Portiono Lurnover Hate	23.68%	24 65%	16 56%								05%
ing the period for which commissions were ch		(1) Computed by dividing the to	to formation of	brokerage c	MA M	that bigg	N/A	ares of inve	AN compa	A/N	A/N	1	<b>≤</b> 1
		ing the period for which com	missions were	charged as	s required b	v the SEC	for fiscal v	nears beauty	ning after	Sentember	1 1005		į
							-		D D				

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 23
Page 1 of 4

## DFA INVESTMENT DIMENSIONS GRO

1299 Ocean Avenue, 11th Floor, Santa Monica, California 90401 Telephone: (310) 395-8005

## STATEMENT OF ADDITIONAL INFORMATION

## March 28, 1997

DFA investment Dimensions Group Inc. (the Fund') offers thirty series of shares. This statement of additional information relates to twenty-four of those series (collectively, the Portfolios'):

U.S. 9-10 Small Company Portfolio
U.S. 6-10 Small Company Portfolio
Enhanced U.S. Large Company Portfolio
U.S. Small Cap Value Portfolio
U.S. Large Cap Value Portfolio
DFA Real Estate Securities Portfolio
Japanese Small Company Portfolio
Pacific Rim Small Company Portfolio
United Kingdom Small Company Portfolio
Emerging Markets Portfolio
Emerging Markets Small Cap Portfolio
DFA Intermediate Government
Fixed Income Portfolio

Continental Small Company Portfolio
Large Cap International Portfolio
U.S. Large Company Portfolio
DFA International Small Cap Value Portfolio
International Small Company Portfolio
DFA One-Year Fixed Income Portfolio
DFA Two-Year Corporate Fixed Income Portfolio
DFA Two-Year Global Fixed Income Portfolio
DFA Two-Year Government Portfolio
DFA Five-Year Government Portfolio
DFA Global Fixed Income Portfolio
DFA Global Fixed Income Portfolio
RWB/DFA International High Book
to Market Portfolio

This statement of additional information is not a prospectus but should be read in conjunction with the Portfolios' prospectus dated March 28, 1997, as amended from time to time, which can be obtained from the Fund by writing to the Fund at the above address or by calling the above telephone number.

## TABLE OF CONTENTS

	Page
PORTFOLIO CHARACTERISTICS AND POLICIES	1
BROKERAGE COMMISSIONS	2
INVESTMENT LIMITATIONS	4
OPTIONS ON STOCK INDICES:	7
FUTURES CONTRACTS	9
FEDERAL TAX TREATMENT OF OPTIONS, FUTURES CONTRACTS AND SIMILAR POSITIONS	9
DIRECTORS AND OFFICERS	10
ADMINISTRATIVE SERVICES	12
OTHER INFORMATION	14
PRINCIPAL HOLDERS OF SECURITIES	15
PURCHASE OF SHARES	19
REDEMPTION AND TRANSFER OF SHARES	19
CALCULATION OF PERFORMANCE DATA	20
FINANCIAL STATEMENTS	. 24

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony_
Schedule 23
Page 2 of 4

from the Series to satisfy the Portfolio's redemption request. Any such redemption to the Portfolio would be in accordance with Rule 18f-1 under the Investment Cor Investors may incur brokerage charges and other transaction costs selling securities to payment of redemptions. The International Equity, DFA Two-Year Global Fixed Income and accordance with Rule 18f-1 under the Investment Cor Schedule Page 2 of payment of redemptions.

Global Fixed Income Portfolios reserve the right to redeem their shares in the currencies in which their investments (and, in respect of the Feeder Portfolios and International Small Company Portfolio, the currencies in which the corresponding Series' investments) are denominated. Investors may incur charges in converting such securities to dollars and the value of the securities may be affected by currency exchange fluctuations.

Shareholders may transfer shares of any Portfolio to another person by making a written request therefore to the Advisor who will transmit the request to the Fund's Transfer Agent. The request should clearly identify the account and number of shares to be transferred, and include the signature of all registered owners and all stock certificates, if any, which are subject to the transfer. The signature on the letter of request, the stock certificate or any stock power must be guaranteed in the same manner as described in the prospectus under "REDEMPTION OF SHARES." As with redemptions, the written request must be received in good order before any transfer can be made.

## CALCULATION OF PERFORMANCE DATA

Following are quotations of the annualized percentage total returns for the one-, five-, and ten-year periods ended November 30, 1996 (as applicable) using the standardized method of calculation required by the SEC, which is net of the cost of any current reimbursement fees charged to investors and paid to the Portfolios. Also included is a quotation of the annualized percentage total return for the DFA Two-Year Global Fixed Income Portfolio (for the period from February 9, 1996, the date of commencement of operations), the Enhanced U.S. Large Company Portfolio (for the period from July 3, 1996, the date of commencement of operations) and the International Small Company Portfolio (for the period from October 1, 1996, the date of commencement of operations) to November 30, 1996 using the standardized method of calculation required by the SEC. Reimbursement fees of 1%, 15% and 15% were in effect from the inception of the Japanese, United Kingdom and Continental Small Company Portfolios, respectively, until June 30, 1995. A reimbursement fee of 1% was in effect from the inception of DFA International Small Cap Value Portfolio until June 30, 1995. Effective June 30, 1995, the amount of the reimbursement fee was reduced with respect to Continental Small Company, Pacific Rim Small Company, Japanese Small Company, Emerging Markets and DFA International Small Cap Value Portfolios, and eliminated with respect to the United Kingdom Small Company Portfolio. The current reimbursement fee for each Portfolio, expressed as a percentage of the net asset value of the shares of the Portfolios, is as follows: Continental Small Company, Pacific Rim Small Company and Emerging Markets Small Cap Portfolios - 1.00%; Japanese Small Company and Emerging Markets Portfolios - 50%; DFA International Small Cap Value Portfolio - .70%; and International Small Company Portfolio - .70%.

A reimbursement fee of 1% was charged to investors in The U.S. 9-10 Small Company Portfolio from December 9, 1986 through June 17, 1988. A reimbursement fee of 0.75% was charged to investors in The Large Cap International Portfolio from the date of its inception until March 5, 1992. In addition, for those Portfolios in effect for less than one, five, or ten years, the time periods during which the Portfolios have been active have been substituted for the periods stated (which in no case extends prior to the effective dates of the Portfolios' registration statements).

	One Year	Five Years	Ten Years
U.S. 9-10 Small Company Portfolio	18.03	20.38	12.35
U.S. 6-10 Small Company Portfolio	18.73	57 Months 13.42	n/a
U.S. Large Company Portfolio	27.48	17.88	71 Months 17.97

U.S. Small Cap Value Portfolio	21.77	Exhibit Contract Te	o. 97-00982 A-SNB stimony 23 of 4
U.S. Large Cap Value Portfolio	22.26	46 Months 16.04	n/a
Enhanced U.S. Large Company Portfolio	4 Months 73.24	n/a	n/a
DFA Real Estate Securities Portfolio	28. <u>2</u> 4	47 Months 9.63	n/a
Japanese Small Company Portfolio	-6.74	-1.07	8 <i>.</i> 58
Pacific Rim Small Company Portfolio	17.87	47 Months 18.01	n/a
United Kingdom Small Company Portfolio	26.74	10.30	10.73
Emerging Markets Portfolio	12.61	31 Months 5.89	n/a
Continental Small Company Portfolio	12.83	5.39	103.5 Months 8.31
Large Cap International Portfolio	12.68	64 Months 8.27	n/a
RWB/DFA International High Book to Market Portfolio	14.60	42 Months 10.62	n/a
DFA One-Year Fixed Income Portfolio	5.91	5.28	6.70
DFA Five-Year Government Portfolio	7.54	6.25	114 Months 7.79
DFA Global Fixed Income Portfolio	11.13	8.40	72 Months 8.83
DFA Intermediate Government Fixed Income Portfolio	4.98	7.89	73 Months 9.37
DFA International Small Cap Value Portfolio	7.24	23 Months 2.08	n/a
DFA Two-Year Global Fixed Income Portfolio	10 Months 7.14	n/a	n/a
International Small Company Portfolio	2 Months -0.40	n/a	n/a

As the following formula indicates, the average annual total return is determined by finding the average annual compounded rates of return over the stated time period that would equate a hypothetical mitial purchase order of \$1,000 to its redeemable value (including capital appreciation/depreciation and dividends and distributions paid and reinvested less any fees charged to a shareholder account) at the end

the stated time period. The calculation assumes that all dividends and distributions are reinvested at the public offering price on the reinvestment dates during the period. The quotation assumes the account was completely redeemed at the end of each period and the deduction of all applicable charges and fees.

Docket No 97-00982 According to the SEC formula:

 $P(1 + T)^n = ERV$ 

where:

P = a hypothetical initial payment of \$1,000

T = average addual total return

n = number of years

ERV = ending redeemable value of a hypothetical \$1,000 payment made at the beginning of the one-, five-, and ten-year periods at the end of the one-, five-, and ten-year periods (or fractional portion thereof).

Following are quotations of the annualized total returns for the one-, five-, and ten-year periods ended November 30, 1996 (as applicable) using a non-standardized method of calculation which is used in communicating performance data in addition to the standardized method required by the SEC. Also included is a quotation of the annualized percentage total return for the DFA Two-Year Global Fixed Income Portfolio (for the period from February 9, 1996, the date of commencement of operations), the Enhanced U.S. Large Company Portfolio (for the period from July 3, 1996, the date of commencement of operations) and the International Small Company Portfolio (for the period from October 1, 1996, the date of commencement of operations) to November 30, 1996 using a non-standardized method of calculation. The non-standardized quotations differ from the standardized in that they are calculated without deduction of any reimbursement fees charged to investors and paid to the Portfolios which would otherwise reduce return quotations for the Portfolios with such fees. Additionally, the non-standardized quotations are presented over time periods which extend prior to the initial investment in the Portfolios (except for The Continental Small Company (and Large Cap International) Portfolios) by using simulated data for the investment strategies of the Portfolios for that portion of the period prior to the initial investment dates. The simulated data excludes the deduction of Portfolio expenses which would otherwise reduce the returns quotations. Non-standardized quotations are also presented for the United Kingdom and Japanese Small Company Portfolios calculated assuming the local currencies of the corresponding Series are invested and redeemed at the beginning and ending dates of the period. The local currency calculations ignore the effect of foreign exchange rates on the investment and only express the returns of the underlying securities of the Series.

	Effective Date/ Initial Investment	One Year	Five Years	Ten Years
U.S. 9-10 Small Company Portfolio	12/22/81 12/22/81	18.03	20.38	12.46
U.S. 6-10 Small Company Portfolio	03/ 06/ 92 03/ 20/ 92	18.73	17.00	11 <i>.</i> 57
U.S. Large Company Portfolio	02/26/90 12/31/90	27.48	17.88	15.02
U.S. Small Cap Value Portfolio	09/ 18/ 92 03/ 01/ 93	21.77	22.14	14.88
U.S. Large Cap Value Portfolio	09/ 18/ 92 02/ 18/ 93	22.26	20.47	15.32

	Docket No. 97-00982
	Exhibit CA-SNB
	Direct Testimony_
	Schedule 24
1	Page 1 of 3
•	

positions generally include listed options on debt securities, options on broad-based on futures contracts, regulated futures contracts and certain foreign currency contracts and options thereon.

Absent a tax election to the contrary, each such Section 1256 position held by a Portfolio or Series will be marked-to-market (i.e., treated as if it were sold for fair market value) on the last business day of a Portfolio's or Series' fiscal year, and all gain or loss associated with fiscal year transactions and marked-to-market positions at fiscal year end (except certain currency gain or loss covered by Section 988 of the Code) will generally be treated as 60% long-term capital gain or loss and 40% short-term capital gain or loss. The effect of Section 1256 marked-to-market rules may be to accelerate income or to convert what otherwise would have been long-term capital gains into short-term capital gains or short-term capital losses into long-term capital losses within a Portfolio or Series. The acceleration of income on Section 1256 positions may require a Portfolio or Series to accrue taxable income without the corresponding receipt of cash. In order to generate cash to satisfy the distribution requirements of the Code, a Portfolio or Series may be required to dispose of portfolio securities that it otherwise would have continued to hold or to use cash flows from other sources such as the sale of a Portfolio's or Series' shares. In these ways, any or all of these rules may affect both the amount, character and timing of income distributed to shareholders by a Portfolio.

When a Portfolio (or in the case of a Feeder Portfolio, the corresponding Series) holds an option or contract which substantially diminishes a Portfolio's or Series' risk of loss with respect to another position of a Portfolio or Series (as might occur in some hedging transactions), this combination of positions could be treated as a "straddle" for tax purposes, resulting in possible deferral of losses, adjustments in the holding periods of a Portfolio's or Series' securities and conversion of short-term capital losses mto long-term capital losses. Certain tax elections exist for mixed straddles (i.e., straddles comprised of at least one Section 1256 position and at least one non-Section 1256 position) which may reduce or eliminate the operation of these straddle rules.

The Portfolios and those Series taxable as regulated investment companies are also subject to the requirement that less than 30% of their annual gross income be derived from the sale or other disposition of securities and certain other investments held for less than three months ("short-short income"). This requirement may limit a Portfolio's (or in the case of a Feeder Portfolio, the corresponding Series') ability to engage in options, straddles, hedging transactions and forward or futures contracts because these transactions are often consummated in less than three months, may require the sale of portfolio securities held less than three months and may, as in the case of short sales of portfolio securities, reduce the holding periods of certain securities within a Portfolio or Series, resulting in additional short-short income for a Portfolio or Series.

A Portfolio (or in the case of a Feeder Portfolio, the corresponding Series) will monitor its transactions in such options and contracts and may make certain other tax elections in order to mitigate the effect of the above rules and to prevent disqualification of a Portfolio or Series as a regulated investment company under Subchapter M of the Code.

## DIRECTORS AND OFFICERS

The names and addresses of the directors and officers of the Fund and a brief statement of their present positions and principal occupations during the past five years is set forth below.

## Directors

David G. Booth\*, 50, Director, President and Chairman-Chief Executive Officer, Santa Monica, CA. President, Chairman-Chief Executive Officer and Director, Dimensional Fund Advisors Inc., DFA Securities Inc., DFA Australia Ltd., Dimensional Investment Group Inc. (registered investment company) and Dimensional Emerging Markets Fund Inc. (registered investment company). Trustee, President and Chairman-Chief Executive Officer of The DFA Investment Trust Company. Chairman and Director, Dimensional Fund Advisors Ltd.

	Docket No. 97-00982
	Exhibit CA-SNB_
	Direct Testimony
,	Schedule 24
	Page 2 of 3

George M. Constantinides, 49, Director, Chicago, IL. L Sched Graduate School of Business, University of Chicago. Trustee, The Page Director, Dimensional Investment Group Inc. and Dimensional Eme

John P. Gould, 58, Director, Chicago, IL. Steven G. Rothmeier Distinguished Service Professor of Economics, Graduate School of Business, University of Chicago. Trustee, The DFA Investment Trust Company and First Prairie Funds (registered investment companies). Director, Dimensional Investment Group Inc., Dimensional Emerging Markets Fund Inc. and Harbor Investment Advisors. Executive Vice President, Lexecon Inc. (economics, law, strategy and finance consulting).

Roger . Ibbotson, 53, Director, New Haven, CT. Professor in Practice of Finance, Yale School of Management. Trustee, The DFA Investment Trust Company. Director, Dimensional Investment Group Inc., Dimensional Emerging Markets Fund Inc., Hospital Fund, Inc. (investment management services) and BIRR Portfolio Analysis, Inc. (software products). Chairman and President, Ibbotson Associates, Inc., Chicago, IL (software, data, publishing and consulting).

Merton H. Miller, 73, Director, Chicago, IL. Robert R. McCormick Distinguished Service Professor Emeritus, Graduate School of Business, University of Chicago. Trustee, The DFA Investment Trust Company. Director, Dimensional Investment Group Inc. and Dimensional Emerging Markets Fund Inc. Public Director, Chicago Mercantile Exchange.

Myron S. Scholes, 55, Director, Greenwich, CT. Limited Partner, Long-Term Capital Management L.P. (money manager). Frank E. Buck Professor of Finance, Graduate School of Business and Professor of Law, Law School, Senior Research Fellow, Hoover Institution, (all) Stanford University (on leave). Trustee, The DFA Investment Trust Company. Director, Dimensional Investment Group Inc., Dimensional Emerging Markets Fund Inc., Benham Capital Management Group of Investment Companies and Smith Breedon Group of Investment Companies.

Rex A. Sinquefield\*, 52, Director, Chairman and Chief Investment Officer, Santa Monica, CA. Chairman-Chief Investment Officer and Director, Dimensional Fund Advisors Inc., DFA Securities Inc., DFA Australia Ltd., Dimensional Investment Group Inc. and Dimensional Emerging Markets Fund Inc. Trustee, Chairman-Chief Investment Officer of The DFA Investment Trust Company. Chairman, Chief Executive Officer and Director, Dimensional Fund Advisors Ltd.

\* Interested Director of the Fund.

## Officers

Each of the officers listed below hold the same office in the following entities: Dimensional Fund Advisors Inc., DFA Securities Inc., DFA Australia Ltd., Dimensional Investment Group Inc., The DFA Investment Trust Company, Dimensional Fund Advisors Ltd., and Dimensional Emerging Markets Fund Inc.

Arthur Barlow, 41, Vice President, Santa Monica, CA.

Maureen Connors, 60, Vice President, Santa Monica, CA.

Truman Clark, 55, Vice President, Santa Monica, CA. Consultant until October 1995 and Principal and Manager of Product Development, Wells Fargo Nikko Investment Advisors, San Francisco, CA from 1990-1994.

Robert Deere, 39, Vice President, Santa Monica, CA.

Irene R. Diamant, 46, Vice President and Secretary (for all entities other than Dimensional Fund Advisors Ltd.), Santa Monica, CA.

Margaret East, 56, Secretary, Dimensional Fund Advisors Ltd.

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 24
Page 3 of 3

Until September, 1995, The DFA Intermediate Government Fixed Income Portfolio was named The DFA Intermediate Government Bond Portfolio, The DFA Global Fixed Income Portfolio was named The DFA Global Bond Portfolio, The Pacific Rim Small Company Portfolio was named The Asia-Australia Small Company Portfolio, The U.S. Large Cap Value Portfolio was named The U.S. Large Cap High Book to Market Portfolio, The U.S. Small Cap Value Portfolio was named The U.S. Small Cap High Book to Market Portfolio, The U.S. 9-10 Small Company Portfolio was named the Small Company Shares. The DFA One-Year Fixed Income Portfolio was named The DFA Fixed Income Shares, and The Continental Small Company Portfolio was named the Continental European Portfolio. Until February, 1996, RWB/DFA International High Book to Market Portfolio was named DFA International High Book to Market Portfolio. From September, 1995 until December, 1996, The DFA Real Estate Securities Portfolio was named DFA/AEW Real Estate Securities Portfolio.

Coopers and Lybrand L.L.P., the Fund's independent accountants, audits the Fund's financial statements.

## PRINCIPAL HOLDERS OF SECURITIES

As of February 28, 1997, the following stockholders owned beneficially at least 5% of the outstanding stock of the Portfolios, as set forth below.

THE U.S. 9-10 SMALL COMPANY PORTFOLIO	
Charles Schwab & Company, Inc REIN*	25.44%
101 Montgomery Street	
San Francisco, CA 94104	
State Farm Insurance Companies	10.76%
One State Farm Plaza	10.76%
Bloomington, IL 61710	
Pepsico Inc. Master Trust	0 D** ##
The Northern Trust Company Trustee	8.87%
P.O. Box 92956	
801 South Canal	
Chicago, IL 60675	
Charles Schwab & Company, Inc REIN* (see address a	bove) 5.97%
Owens-Illinois	5.48%
Master Retirement Trust	J.4676
34 Exchange Place	
Jersey City, NJ 07302	
National Electrical Benefit Fund	***
1125 15th Street NW	5.26%
Washington, DC 20005	
THE U.S. 6-10 SMALL COMPANY PORTFOLIO	
McKinsey & Company Master Retirement Trust	26.42.77
55 E 52nd Street	26.43%

55 E. 52nd Street New York, NY 10055

# Data on Dr. Andrews' Companies

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 25
Page 1 of 1

* Excludes Washington On O			Average	Tankee Energy System, Inc	validy resources, Inc	Valley Recourses In-	United Cities Gas Company	Courreastern Michigan Gas Enterprises, Inc	South Control March Control Ma	Providence Energy Company	Pennsylvania Enterprises, Inc	rubiic Service Company of North Carolina, Incorporated	Dishing Social Cas Company	Northwest Natural Cas Corporation	North Carolina Natural Gas Composition	Mobile Gas Service Corporation	chergy west incorporated		Energy North Inc	Energen Corporation	Essex County Gas Company	Fig. 1 Valuidi Gas Company, Inc	Delta Natural Con Computation	Chesapeake Utilities Company	Colonial Gas Company	Cascade Natural Gas Corporation	Cay State Gas Company	Ray State Care Company	Berkshire Cas Composition	Atmos Energy Corporation		3		COMPANY NAME *	
	4	\$20.30	\$21 13		\$10 05	\$21 50	61/20	617 60	\$17 75	\$22 13	<b>*</b> 17 KJ	\$17 25	\$24 25	\$29 63	\$26 /5	30 20	\$8 KO	\$21 75	\$30 50	CZ 42¢	9 1 0	<b>\$</b> 16.63	<b>\$16</b> 75	\$20 00	\$10.30	#10 00	\$35 50	<b>\$</b> 15 13	<b>\$</b> 22 63			(2)		4/30/97	PRICE
	0007	9967	10450	4200	Ance .	13221	13020	1000	5767	9608	96761	10000	22 <u>566</u>	6613	3228	/35/	777	3244	13027	1667	6363	3050	4453	8518	10824	10409	13.50	2177	16135			(3)	,	OUTSTANDING (000)	STOCK
	7,852	10,100	28.499	2824		7681	8,509	200,0	B 0E 3	6 627	11,500	0,009	10 860	5 094	1,624	1,600	2,300	300	7.700	1,336	2,382	222	2213	5931	10840	10,820	1,001	1 001	28 624			4		SHARE	NUM OF
	1371	307	367	1511	1771	1704	1530	953	350	1450	1678	2078	0621	1200	1988	1473	1410	1032	1602	1248	976	2012	2 -1-2	1436	999	1242	1157	¥0	F 0.4	[cor (3) / col (4)]	_	(5)	O CONTOURK	SHARES PER	
	<b>\$</b> 28.195	\$7,746	* 10,000 10,000	\$18 505	\$37,007	250,036	\$36 803	\$16,914	\$32,077	90,010	\$28 Q45	\$50,394	\$38,459	\$33, I / I	662 474	\$12 522	\$30,677	\$51,600	\$54,200 \$54,200	\$30.258	\$16.227	\$33,704	\$28,724	#10,331	#15 251	\$31.671	<b>\$17</b> ,505	\$12,753		[col (2) X col (5)]	(0)	(e)	4/30/97	SHAREHOLDER	VALUE OF
190	100	221	52	ָרָ לְּנָי	284	229	0 6	103	213	333	) ) )	547	1 <b>9</b> 6	86	20	3 :	71	397	40	, S	30	75	170	1//7	ì	343 343	ين ند	365		[col (2) X col (3)]	(7)	į	4/30/97 \$(Millions)	MARKET VALUE	

<sup>\*</sup> Excludes Washington Gas Company
It Merged With an Electric Power Company

# Gas Company Stocks Owned by the DFA 9-10 Fund

Did the US 9-10 Small Company Mutual Fund Own Stock in Dr Andrews' Comparable Companies? YEAR

COMPANY

	TOTAL INCLUDED IN PORTFOLIO  9	Atmos Energy Corporation Berkshire Gas Company Bay State Gas Company Cascade Natural Gas Corporation Chesapeake Utilities Corporation Colonial Gas Company Delta Natural Gas Company, Inc. Energen Corporation Energy West Incorporated Essex County Gas Company Mobile Gas Service Corporation North Carolina Natural Gas Company Pennsylvania Enterprises, Inc. Providence Energy Corporation Northwest Natural Gas Company Pennsylvania Enterprises, Inc. Providence Energy Corporation North Carolina Nichigan Gas Enterprises, Inc United Cities Gas Company Valley Resources, Inc. YES NO TOTAL NOT INCLUDED IN BORTER  NO TOTAL NOT INCLUDED IN BORTER  NO NO NO NO TOTAL NOT INCLUDED IN BORTER  NO NO NO NO NO NO NO TOTAL NOT INCLUDED IN BORTER  NO	
S.		NO YES	2
	11	NO N	

SOURCE 1994 & 1996 - DFA ANNUAL REPORT SOURCE 1995 10K REPORT

Docket No 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 26

Page 1 of 1

Table A-1

## Large Company Stocks: Total Returns

(continued)

Docket No. 97-00982 Exhibit CA-SNB\_\_\_\_ Direct Testimony\_\_\_ Schedule 27\_\_\_\_ Page 1 of 1\_\_\_\_

## From January 1971 to December 1995

YEAR	MAL	FEB	MAR	APR	MAY	HUL	JUL	AUG	SEP	OCT	NOV	DEC	YEAR	JAN-DEC.
1971	0 0419	0 0141	0 0382	0 0377	-0 0367	0 0021	-0 0399	0 0412	-0 0056	-0 0404	0 0027	0 0877	1971	0 1431
1972	0.0194	0.0299	0 0072	0 0057	0 0219	-0 0205	0 0036	0 0391	-0 0036	0 0107	0 0505	0 0131	1972	0 1898
1973	-0 0159	-0 0333	-0 0002	-0 0395	-0 0139	-0 0051	0 0394	-0 0318	0 0415	0 0003	-0 1082	0 0183	1973	-0 1466
1974	-0.0085	0 0019	-0.0217	-0 0373	-0 0272	-0 0128	-0 0759	-0 0828	-0 1170	0 1657	-0 0448	-0 0177	1974	-0.2647
1975	0.1251	0 0674	0 0237	0 0493	0 0509	0 0462	-0 0659	-0 0144	-0 0328	0 0637	0 0313	-0 0096	1975	0 3720
1976	0 1199	-0 0058	0 0326	-0 0099	-0 0073	0 0427	-0 0068	0 0014	0 0247	-0 0206	-0 0009	0 0540	1976	0.2384
1977	-0 0489	-0 0151	-0 0119	0 0014	-0 0150	0 0475	-0 0151	-0 0133	0 0000	-0 0415	0 0370	0 0048	1977	-0 0718
1978	-0 0596	-0 0161	0.0276	0 0870	0 0136	-0 0152	0 0560	0 0340	-0 0048	-0 0891	0 0260	0 0172	1978	0.0656
1979	0 0421	-0 0284	0 0575	0 0036	-0 0168	0 0410	0 0110	0 0611	0 0025	-0 0656	0 0514	0 0192	1979	0 1844
1980	0 0610	0 0031	-0 0987	0 0429	0 0562	0.0296	0 0676	0 0131	0 0281	0 0187	0 1095	-0 0315	1980	0.3242
1981	-0 0438	0 0208	0 0380	-0 0213	0 0062	-0 0080	0 0007	-0 0554	-0 0502	0 0528	0 0441	-0 0265	1981	-0 0491
1982	-0 0163	-0 0512	-0 0060	0 0414	-0 0288	-0 0174	-0 0215	0 1267	0 0110	0 1126	0 0438	0 0173	1982	0 2141
1983	0 0348	0 0260	0 0365	0 0758	-0 0052	0 0382	-0 0313	0 0170	0 0136	-0 0134	0 0233	-0 0061	1983	0.2251
1984	-0 0065	-0 0328	0 0171	0 0069	-0 0534	0 0221	-0 0143	0 1125	0 0002	0 0026	-0.0101	0.0253	1984	0 0627
1985	0 0768	0 0137	0 0018	-0 0032	0 0615	0 0159	-0 0026	-0 0061	-0 0321	0 0447	0 0716	0 0467	1985	0 3216
1986	0 0044	0 0761	0 0554	-0 0124	0 0549	0 0166	-0 0569	0 0748	-0 0822	0 0556	0 0256	-0 0264	1986	
1987	0 1343	0 0413	0 0272	-0 0088	0 0103	0 0499	0 0498	0 0385	-0 0220	-0 2152	-0 0819	0 0738	1987	
1988	0 0427	0.0470	-0 0302	0 0108	0 0078	0.0464	-0 <b>00</b> 40	-0 0331	0 0424	0 0273	-0 0142	0.0181	1988	
1989	0 0723	-0 0249	0 0236	0 0516	0 0402	-0 0054	0 0898	0 0193	-0 0039	-0 0233	0 0208	0 0236	1989	0 3149
1990	-0 0671	0 0129	0 0263	-0 0247	0 0975	-0 0070	-0 0032	-0 0903	-0 0492	-0 0037	0 0644	0.0274	1990	-0 0317
1991	0 0442	0 0716	0 0238	0 0028	0 0428	-0 0457	0 0468	0 0235	-0 0164	0 0134	-0 0404	0 1143	1991	
1992	-0,0186	0 0128	-0 0196	0 0291	0 0054	-0 0145	0 0403	-0 0202	0 0115	0 0036	0 0337	0 0131	1992	
1993	0 0073	0 0135	0 0215	-0 0245	0 0270	0 0033	-0 0047	0 0381	-0 0074	0 0203	-0 0094	0 0123	1993	
1994	0 0335	-0 0270	-0 0435	0 0130	0 0163	-0 0247	0 0331	0 0407	-0 0241	0 0229	-0 0367	0 0146	1994	
1995	0 0260	0 0388	0 0296	0 0291	0 0395	0 0235	0 0333	0 0027	0 0419	-0 0035	0 0440	0 0185	1995	0 3743

<sup>\*</sup> Compound annual return

Docket No. 97-00982
Exhibit CA-SNB
Direct Testimony
Schedule 28
Page 1 of 1

Office of the Consumer Advocate Interrogatory/Data Request-7/8/97

- Q.47. Regarding the results of Dr. Andrew's regression analysis shown in Schedule 9, produce the T-statistic for each company's alpha and the T-statistic for each company's beta.
- A.47. The results of regressions performed on the data for each company listed in Schedule 9 are employed only in summary, aggregated form as average alphas and betas. The average alpha and average beta are analogous to the alpha and beta of a portfolio of common stocks, in this case a "portfolio" of 22 small gas LDC's. Tests of significance, such as T-statistics, from the regressions related to individual stocks intrinsically cannot be summed or averaged across the composite (or portfolio). Accordingly, they were not found in company with the individual regressions and, hence, cannot be supplied as requested.

Signature

Victor L. Andrews, President, Andrews Financial Associates, Inc.

## APPENDIX A

## IBBOTSON YEARBOOK'S HYPOTHETICAL DISTRIBUTION OF RETURNS

The derivation of Schedule 12 and Charts two and three is based on the same probability principles used in the example shown in SBBI-97 at pages 154-155. Those pages are attached to and are part of this appendix as Attachments 1 and 2. The hypothetical distribution in the example assumes:

10% is the size of the loss

30% is the size of the gain

50% is the probability of a loss

50% is the probability of a gain.

Starting with an investment of \$1, after 1 year there are two possible values, the investment will be worth either \$1.3 or 90 cents. After two years there are 4 possibilities, one at \$1.69, two outcomes at \$1.17 and one at \$.81. This shows that the number of possibilities double each year. The example is well-grounded in mathematics and is a simple illustration of a mathematical formula that is over 500 years old. If \$1.3 is treated as X and \$.9 is treated as Y, the first year after the investment the possible outcomes are:

$$(X + Y)^{1} = 1(\$1.3) + 1(\$.9)$$

In the second year after the investment the possible outcomes are:

$$(X + Y)^2 = 1(X^2) + 2(XY) + 1(Y^2)$$

Docket No. 97-00982. CA-Brown, Appendix A of Direct Testimony

$$(\$1.3 + \$.9)^2 = 1(\$1.69) + 2(\$1.17) + 1(\$.81)$$

The underlined values -- 1 and 1 in the first year and 1, 2, 1 in the second year -- match the total number of possibilities - 2 in the first year and 4 in the second, and the values in the parentheses -- \$1.3 and \$.9 in the first year and \$1.69, \$1.17, \$.81 in the second -- represent the values of the possibilities. There are two important aspects of the example especially in the second year: the geometric mean is the middle value, \$1.17, which has a corresponding annual return of 8.2%, is the most likely outcome - 2 chances out of four. Three out of the four chances, 75% of the possibilities, are at or below the middle value. The odds are only 25% that the investment will reach the average of \$1.21, which has a corresponding return of 10%.

The heart of the example can be restated.

This information about a distribution:

10% is the size of the loss

30% is the size of the gain

50% is the probability of a loss

50% is the probability of a gain.

Leads to these facts about the distribution:

an 8.2% return is the distribution's middle

a 10% return is the distribution's average

And

the number of possibilities doubles as the "years increase: in the first year there are 2

Docket No. 97-00982. CA-Brown, Appendix A of Direct Testimony

possibilities, 4 in the second, 8 in the third and so forth.

By the time 71 years elapse from 1925 to 1996 the equation above changes to:

$$(X + Y)^{71}$$

Although this term is huge it can be calculated easily with computers, giving the total number of possibilities and the possibilities for each outcome. Attachments 3 and 4 show the possibilities each year, the symmetrical pattern each year and the distribution in percentage terms. The patterns do not depend on the values of X and Y. No matter what values X and Y are, the pattern of possibilities is the same. This is why Chart 3 in my direct testimony is also symmetrical.

## ACTUAL DISTRIBUTION OF LARGE COMPANY RETURNS: 1925-1996

Ibbotson's data on large companies covers 71 years. It shows a return of 10.7% as being in the middle of the distribution and an average of return of 12.7%. This is different than the example in the sense that the order of the information is reversed from the example.

The information about the actual distribution:

a 10.7% return is the distribution's middle

a 12.7% return is the distribution's average

50% is the probability of a loss

50% is the probability of a gain.

Leads to these questions about the actual distribution:

What percentage is the size of the loss?
What percentage is the size of the gain?

I calculated the size of the loss to be 8.3% and the size of the gain to be 33.6%. These are the first and last values in column (3) of Schedule 12. I then applied these two figures to the formula

$$(X + Y)^{71}$$

This gives the total number of possible returns, the value of each return, and the probability of each return in 1996 - given a \$1 investment in 1925. This is the data shown in Schedule 12.

The Schedule indicates that the average return, 12.7%, has a less then 20% chance of being achieved in 1996. If the odds were looked at in 1927, the second year after the investment, the chance of achieving the average return would be no more than 25%. The point here is that as time progresses, the average return has a little less of a chance of being achieved. Its odds shrink from no more than 25% in the second year to less than 20% in the 71st year. This is not much of a change, but it highlights why the average return is not considered a useful measure by the sources I quoted. The average return is not the midpoint of the distribution, and the average return gets further and further away from the midpoint as time progresses.

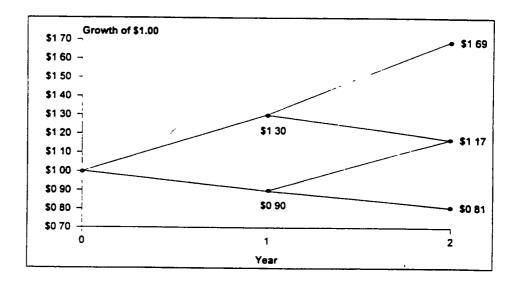
Appendix A of \_\_\_\_\_ Direct Testimony Docket No. 97-00982 Exhibit CA-SNB\_\_\_\_ Attachment 1

where the cost of capital is the sum of its parts. Therefore, the CAPM expected equity risk premium must be derived by arithmetic, not geometric, subtraction.

## Anthmetic Versus Geometric Means

The expected equity risk premium should always be calculated using the arithmetic mean. The anthmetic mean is the rate of return which, when compounded over multiple periods, gives the mean of the probability distribution of ending wealth values. (A simple example given below shows that this is true.) This makes the arithmetic mean return appropriate for computing the cost of capital. The discount rate that equates expected (mean) future values with the present value of an investment is that investment's cost of capital. The logic of using the discount rate as the cost of capital is reinforced by noting that investors will discount their expected (mean) ending wealth values from an investment back to the present using the arithmetic mean, for the reason given above. They will, therefore, require such an expected (mean) return prospectively (that is, in the present looking toward the future) to commit their capital to the investment.

For example, assume a stock has an expected return of +10 percent in each year and a standard deviation of 20 percent. Assume further that only two outcomes are possible each year— +30 percent and -10 percent (that is, the mean plus or minus one standard deviation), and that these outcomes are equally likely. (The arithmetic mean of these returns is 10 percent, and the geometric mean is 8.2 percent.) Then the growth of wealth over a two-year period occurs as shown below.



Note that the median (middle outcome) and mode (most common outcome) are given by the geometric mean, 8.2 percent, which compounds up to 17 percent over a 2-year period (hence a terminal wealth of \$1.17). However, the expected value, or probability-weighted average of all possible outcomes, is equal to:

	(.25	×	1.69)	=	0.4225
+	(.50	×	1.17)	=	0.5850
+	(.25	×	0.81)	= '	0.2025
TOTAL					1.2100

Now, the rate that must be compounded up to achieve a terminal wealth of \$1.21 after 2 years is 10 percent; that is, the expected value of the terminal wealth is given by compounding up the *arithmetic*, not the geometric mean. Since the arithmetic mean equates the expected future value with the present value, it is the discount rate.

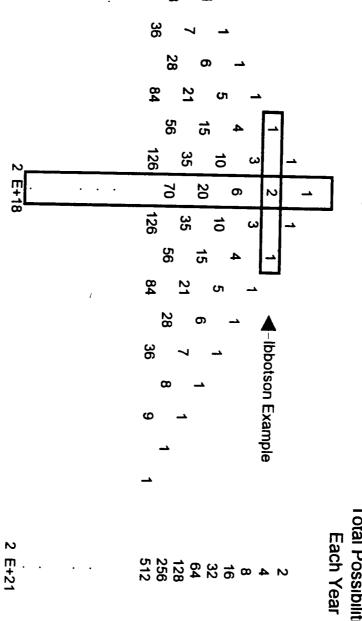
Stated another way, the arithmetic mean is correct because an investment with uncertain returns will have a higher expected ending wealth value than an investment that earns, with certainty, its compound or geometric rate of return every year. In the above example, compounding at the rate of 8.2 percent for two years yields a terminal wealth of \$1.17, based on \$1.00 invested. But holding the uncertain investment, with a possibility of high returns (two +30 percent years in a row) as well as low returns (two -10 percent years in a row), yields a higher expected terminal wealth, \$1.21. In other words, more money is gained by higher-than-expected returns than is lost by lower-than-expected returns. Therefore, in the investment markets, where returns are described by a probability distribution, the arithmetic mean is the measure that accounts for uncertainty, and is the appropriate one for estimating discount rates and the cost of capital.

Arbitrage Pricing
Theory

APT is a model of the expected return on a security. It was originated by Stephen A. Ross, and elaborated by Richard Roll. APT treats the expected return on a security (i.e., its cost of capital) as the sum of the payoffs for an indeterminate number of risk factors, where the amount of each risk factor inherent in a given security is estimated. Like the CAPM, APT is a model that is consistent with equilibrium and does not attempt to outguess the market. APT

## Distribution of Possibilities for (X + Y)

Center of the Distribution



765432

**Total Possibilities** 

Docket No. 97-00982 Exhibit CA-SNB\_\_\_\_\_ Attachment 3

, ,

71

## Distribution of Possibilities for (X + Y) As a Percent of Possibilities Center of the Distribution

Appendix A of

3% 7% 6% 16% 16% 22% 23% 25% 27% 25% 31% 38% 50% 27% 31% 38% 100% 31% 25% 50% 38% 22% 23% 25% 16% 16% 16% 13% 11% 9% 6% Ibbotson Example 3% 2% 2% **%** 0% 0% **Total Possibilities** Each Year 8 16 32 64 128 256 512 Attachment 4 Exhibit CA-SNB\_ Direct Testimony
Docket No 97-00982

a)

**o** ≺

0%

2%

9%

2. E+21

71

တေ

765432

0%